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CONTEXT c_sd_bolus

SETS

SD

SDF

CONSTANTS

deliver

off

suspend

preempt

s

d

AXIOMS

axm1: $partition(SD, \{deliver\}, \{off\}, \{suspend\}, \{preempt\})$

axm2: $partition(SDF, \{s\}, \{d\})$

END

CONTEXT c_bolus

SETS

BOLUS_STATUS

CONSTANTS

null

normal

square

dual

AXIOMS

axm1: $partition(BOLUS_STATUS, \{null\}, \{normal\}, \{square\}, \{dual\})$

END

CONTEXT c_normalbolus

CONSTANTS

normal_bolus_rate

AXIOMS

axm1: $normal_bolus_rate > 0$

END

CONTEXT c_normalbolus_anim

EXTENDS c_normalbolus

AXIOMS

axm1: $normal_bolus_rate = 2$

END

CONTEXT c_basal

SETS

BASALMODE

CONSTANTS

basal_max

c

suspended

delivering

stop

AXIOMS

axm1: $basal_max \in \mathbb{N}_1$

axm2: $c = 48$

axm3: $partition(BASALMODE, \{suspended\}, \{delivering\}, \{stop\})$

END

CONTEXT c_basal2

EXTENDS c_basal

SETS

PROG0

CONSTANTS

null

call_get_min

return_get_min

call_get_max

return_get_max

PROC_BASAL

AXIOMS

axm2: $PROC_BASAL \subseteq PROG0$

axm1: $partition(PROC_BASAL, \{null\}, \{call_get_min\}, \{return_get_min\}, \{call_get_max\}, \{return_get_max\})$

END

CONTEXT c_basal2_USER_anim

EXTENDS c_basal2

CONSTANTS

bsuspend

bresume

AXIOMS

axm1: $bsuspend = 3$

axm2: $bresume = 8$

END

MACHINE Square

SEES c_sd_bolus

VARIABLES

state

INVARIANTS

inv1: $state \in SD$

EVENTS

Initialisation

begin

act1: $state := off$

end

Event start ⟨ordinary⟩ $\hat{=}$

when

grd1: $state = off$

then

act1: $state := deliver$

end

Event finish ⟨ordinary⟩ $\hat{=}$

when

grd1: $state = deliver$

then

act1: $state := off$

end

Event suspend ⟨ordinary⟩ $\hat{=}$

when

grd1: $state = deliver$

then

act1: $state := suspend$

end

Event resume ⟨ordinary⟩ $\hat{=}$

when

grd1: $state = suspend$

then

act1: $state := off$

end

Event preempted ⟨ordinary⟩ $\hat{=}$

when

grd1: $state = deliver$

then

act1: $state := preempt$

end

Event resume_from_preempt ⟨ordinary⟩ $\hat{=}$

when

grd1: $state = preempt$

then

act1: $state := deliver$

end

END

MACHINE Square1**REFINES** Square**SEES** c_sd_bolus**VARIABLES**

state
s_r
s_t
s_deliver_time
s_deliver_rate

INVARIANTS

inv1: $s_r \in \mathbb{N}$
inv2: $s_t \in \mathbb{N}$
inv3: $s_deliver_time \in \mathbb{N}$
inv4: $s_deliver_rate \in \mathbb{N}$
inv5: $state = off \vee state = suspend \Rightarrow s_deliver_time = 0 \wedge s_deliver_rate = 0$
inv6: $state = deliver \Rightarrow s_deliver_time \geq 0 \wedge s_deliver_rate > 0$
inv7: $state = preempt \Rightarrow s_deliver_time \geq 0 \wedge s_deliver_rate = 0$
inv8: $state = off \vee state = suspend \Rightarrow s_r = 0 \wedge s_t = 0$
inv9: $state = deliver \vee state = preempt \Rightarrow s_r > 0$
inv10: $state = deliver \vee state = preempt \Rightarrow s_t > 0$

EVENTS**Initialisation** ⟨extended⟩**begin**

act1: $state := off$
act2: $s_r := 0$
act3: $s_t := 0$
act4: $s_deliver_time := 0$
act5: $s_deliver_rate := 0$

end**Event** start ⟨ordinary⟩ $\hat{=}$ **extends** start**any**

t
r

where

grd1: $state = off$
grd2: $t \in \mathbb{N}_1$
grd3: $r \in \mathbb{N}_1$

then

act1: $state := deliver$
act2: $s_r := r$
act3: $s_t := t$
act4: $s_deliver_time := t$
act5: $s_deliver_rate := r$

end**Event** finish ⟨ordinary⟩ $\hat{=}$ **extends** finish**when****grd1:** $state = deliver$ **then**

act1: $state := off$
act2: $s_deliver_time := 0$
act3: $s_deliver_rate := 0$
act4: $s_r := 0$
act5: $s_t := 0$

```

    end
Event suspend ⟨ordinary⟩ ≐
extends suspend
    when
        grd1: state = deliver
    then
        act1: state := suspend
        act2: s.deliver_time := 0
        act3: s.deliver_rate := 0
        act4: s.r := 0
        act5: s.t := 0
    end
Event resume ⟨ordinary⟩ ≐
extends resume
    when
        grd1: state = suspend
    then
        act1: state := off
    end
Event preempted ⟨ordinary⟩ ≐
extends preempted
    any
        t time left for square bolus
    where
        grd1: state = deliver
        grd2: t ∈ ℕ
    then
        act1: state := preempt
        act2: s.deliver_time := t
        act3: s.deliver_rate := 0
    end
Event resume_from_preempt ⟨ordinary⟩ ≐
extends resume_from_preempt
    when
        grd1: state = preempt
    then
        act1: state := deliver
        act3: s.deliver_rate := s.r
    end
END

```

MACHINE Square_Dual_bolus2**REFINES** Square1**SEES** c_sd_bolus,c_normalbolus**VARIABLES**

state
s_r
s_t
d_deliver_time
d_deliver_rate
d_t
sd_module
sd_flag

INVARIANTS

inv1: $d_deliver_time \in \mathbb{N}$
inv2: $d_deliver_rate \in \mathbb{N}$
inv3: $d_t \in \mathbb{N}$
inv4: $sd_module \in SDF$
inv5: $sd_flag \in SDF$
inv6: $state = off \vee state = suspend \Rightarrow d_deliver_time = 0 \wedge d_deliver_rate = 0$
inv7: $state = deliver \Rightarrow d_deliver_time \geq 0 \wedge d_deliver_rate > 0$
inv8: $state = off \vee state = suspend \Rightarrow d_t = 0$
inv9: $state = deliver \vee state = preempt \Rightarrow s_r > 0$
inv10: $state = preempt \Rightarrow d_deliver_time \geq 0 \wedge d_deliver_rate = 0$
inv11: $sd_module = d \wedge sd_flag = s \wedge state = deliver \Rightarrow d_deliver_rate = s_r$
inv12: $sd_module = d \wedge sd_flag = d \wedge state = deliver \Rightarrow d_deliver_rate = normal_bolus_rate$
inv13: $sd_module = s \wedge state = deliver \Rightarrow d_deliver_rate = s_r$
inv14: $state = off \vee state = suspend \Rightarrow sd_flag = d$
Square1.inv1: $s_r \in \mathbb{N}$
Square1.inv2: $s_t \in \mathbb{N}$
Square1.inv3: $s_deliver_time \in \mathbb{N}$
Square1.inv4: $s_deliver_rate \in \mathbb{N}$
Square1.inv8: $state = off \vee state = suspend \Rightarrow s_r = 0 \wedge s_t = 0$
Square1.inv10: $state = deliver \vee state = preempt \Rightarrow s_t > 0$
Square.inv1: $state \in SD$

EVENTS**Initialisation****begin**

act1: $state := off$
act2: $s_r := 0$
act3: $s_t := 0$
act6: $d_deliver_time := 0$
act7: $d_deliver_rate := 0$
act8: $d_t := 0$
act9: $sd_module := s$
act10: $sd_flag := d$

end**Event** start (ordinary) $\hat{=}$ **refines** start**any**

t
r

where

grd1: $state = off$
grd2: $t \in \mathbb{N}_1$

```

    grd3:  $r \in \mathbb{N}_1$ 
  then
    act1:  $state := deliver$ 
    act2:  $s.r := r$ 
    act3:  $s.t := t$ 
    act6:  $sd\_module := s$ 
    act7:  $d.deliver\_time := t$ 
    act8:  $d.deliver\_rate := r$ 
  end
Event start_dual ⟨ordinary⟩  $\hat{=}$ 
refines start
  any
    t
    r
    td
  where
    grd1:  $state = off$ 
    grd2:  $t \in \mathbb{N}_1$ 
    grd3:  $r \in \mathbb{N}_1$ 
    grd4:  $td \in \mathbb{N}_1$ 
  then
    act1:  $state := deliver$ 
    act2:  $s.r := r$ 
    act3:  $s.t := t$ 
    act6:  $d.deliver\_time := t + td$ 
    act7:  $d.deliver\_rate := normal\_bolus\_rate$ 
    act8:  $d.t := td$ 
    act9:  $sd\_module := d$ 
  end
Event update_to_dual ⟨ordinary⟩  $\hat{=}$ 
  when
    grd2:  $state = deliver$ 
    grd3:  $sd\_module = d$ 
    grd4:  $sd\_flag = d$ 
  then
    act2:  $d.deliver\_rate := s.r$ 
    act3:  $sd\_flag := s$ 
  end
Event finish ⟨ordinary⟩  $\hat{=}$ 
refines finish
  when
    grd1:  $state = deliver$ 
    grd2:  $sd\_module = d \Rightarrow sd\_flag = s$ 
  then
    act1:  $state := off$ 
    act4:  $s.r := 0$ 
    act5:  $s.t := 0$ 
    act6:  $d.deliver\_time := 0$ 
    act7:  $d.deliver\_rate := 0$ 
    act8:  $d.t := 0$ 
    act9:  $sd\_flag := d$ 
  end
Event suspend ⟨ordinary⟩  $\hat{=}$ 
refines suspend
  when
    grd1:  $state = deliver$ 
  then
    act1:  $state := suspend$ 

```

```

    act4:  $s_r := 0$ 
    act5:  $s_t := 0$ 
    act6:  $d\_deliver\_time := 0$ 
    act7:  $d\_deliver\_rate := 0$ 
    act8:  $d_t := 0$ 
    act9:  $sd\_flag := d$ 
  end
Event resume ⟨ordinary⟩  $\hat{=}$ 
extends resume
  when
    grd1:  $state = suspend$ 
  then
    act1:  $state := off$ 
  end
Event preempted ⟨ordinary⟩  $\hat{=}$ 
refines preempted
  any
    t time left for square bolus
  where
    grd1:  $state = deliver$ 
    grd2:  $t \in 0 .. d\_deliver\_time$ 
  then
    act1:  $state := preempt$ 
    act4:  $d\_deliver\_time := t$ 
    act5:  $d\_deliver\_rate := 0$ 
  end
Event resume_from_preempt ⟨ordinary⟩  $\hat{=}$ 
refines resume_from_preempt
  any
    r
  where
    grd1:  $state = preempt$ 
    grd2:  $sd\_module = s \Rightarrow r = s_r$ 
    grd3:  $sd\_module = d \wedge sd\_flag = d \Rightarrow r = normal\_bolus\_rate$ 
    grd4:  $sd\_module = d \wedge sd\_flag = s \Rightarrow r = s_r$ 
  then
    act1:  $state := deliver$ 
    act4:  $d\_deliver\_rate := r$ 
  end
END

```

MACHINE Square_Dual_bolus2_continuous**REFINES** Square_Dual_bolus2**SEES** c_sd_bolus,c_normalbolus**VARIABLES**

state
 s_r
 s_t
 d_deliver_time
 d_deliver_rate
 d_t
 sd_module
 sd_flag
 sd_now
 sd_new_now
 sd_rate_c

INVARIANTS**inv5:** $sd_rate_c \in \mathbb{N} \leftrightarrow \mathbb{N}$ **inv1:** $sd_now \in dom(sd_rate_c)$ **inv2:** $sd_new_now \in \mathbb{N}$ **inv4:** $d_deliver_rate = sd_rate_c(sd_now)$ **inv6:** $state \in \{deliver, preempt\} \wedge sd_module = d \wedge sd_flag = d \Rightarrow d_deliver_time > s_t$ **EVENTS****Initialisation** ⟨extended⟩**begin**

act1: $state := off$
act2: $s_r := 0$
act3: $s_t := 0$
act6: $d_deliver_time := 0$
act7: $d_deliver_rate := 0$
act8: $d_t := 0$
act9: $sd_module := s$
act10: $sd_flag := d$
act11: $sd_now := 0$
act12: $sd_new_now := 0$
act13: $sd_rate_c := \{0 \mapsto 0\}$

end**Event** start ⟨ordinary⟩ $\hat{=}$ **extends** start**any**

t
 r
 ctime

where

grd1: $state = off$
grd2: $t \in \mathbb{N}_1$
grd3: $r \in \mathbb{N}_1$
grd4: $ctime \geq sd_now$

then

act1: $state := deliver$
act2: $s_r := r$
act3: $s_t := t$
act6: $sd_module := s$
act7: $d_deliver_time := t$
act8: $d_deliver_rate := r$
act9: $sd_rate_c := \lambda x \cdot x \in ctime .. ctime + t | r$
act10: $sd_now := ctime$

```

    act11: sd_new_now := ctime + t
  end
Event start_dual ⟨ordinary⟩ ≐
extends start_dual
  any
    t
    r
    td
    ctime
  where
    grd1: state = off
    grd2:  $t \in \mathbb{N}_1$ 
    grd3:  $r \in \mathbb{N}_1$ 
    grd4:  $td \in \mathbb{N}_1$ 
    grd5:  $ctime \geq sd\_now$ 
  then
    act1: state := deliver
    act2: s.r := r
    act3: s.t := t
    act6: d.deliver_time := t + td
    act7: d.deliver_rate := normal_bolus_rate
    act8: d.t := td
    act9: sd_module := d
    act11:  $sd\_rate\_c := \lambda x \cdot x \in ctime .. ctime + td | normal\_bolus\_rate$ 
    act12: sd_now := ctime
    act10: sd_new_now := ctime + td
  end
Event finish ⟨ordinary⟩ ≐
extends finish
  any
    ctime
  where
    grd1: state = deliver
    grd2:  $sd\_module = d \Rightarrow sd\_flag = s$ 
    grd3:  $ctime = sd\_new\_now$ 
  then
    act1: state := off
    act4: s.r := 0
    act5: s.t := 0
    act6: d.deliver_time := 0
    act7: d.deliver_rate := 0
    act8: d.t := 0
    act9: sd_flag := d
    act10:  $sd\_rate\_c := \lambda x \cdot x \geq ctime | 0$ 
    act11: sd_now := ctime
  end
Event suspend ⟨ordinary⟩ ≐
extends suspend
  any
    ctime
  where
    grd1: state = deliver
    grd2:  $ctime \in sd\_now .. sd\_new\_now$ 
  then
    act1: state := suspend
    act4: s.r := 0
    act5: s.t := 0
    act6: d.deliver_time := 0

```



```

    act7: d_deliver_rate := 0
    act8: d_t := 0
    act9: sd_flag := d
    act10: sd_now := ctime
    act11: sd_rate_c :=  $\lambda x \cdot x \geq ctime$ |0
  end
Event resume ⟨ordinary⟩  $\hat{=}$ 
extends resume
  any
    ctime
  where
    grd1: state = suspend
    grd2: ctime > sd_now
  then
    act1: state := off
    act2: sd_now := ctime
    act3: sd_rate_c :=  $\lambda x \cdot x \geq ctime$ |0
  end
Event preempted ⟨ordinary⟩  $\hat{=}$ 
extends preempted
  any
    t time left for square bolus
    ctime
  where
    grd1: state = deliver
    grd2:  $t \in 0 .. d\_deliver\_time$ 
    grd3:  $ctime \in sd\_now .. sd\_new\_now$ 
    grd4:  $sd\_module = d \wedge sd\_flag = d \Rightarrow t \in s.t + 1 .. d\_deliver\_time$ 
    grd5:  $sd\_module = d \wedge sd\_flag = s \Rightarrow t \in 0 .. s.t$ 
  then
    act1: state := preempt
    act4: d_deliver_time := t
    act5: d_deliver_rate := 0
    act6: sd_now := ctime
    act7: sd_rate_c :=  $\lambda x \cdot x \geq ctime$ |0
  end
Event resume_from_preempt ⟨ordinary⟩  $\hat{=}$ 
extends resume_from_preempt
  any
    r
    ctime
    t2
  where
    grd1: state = preempt
    grd2:  $sd\_module = s \Rightarrow r = s\_r$ 
    grd3:  $sd\_module = d \wedge sd\_flag = d \Rightarrow r = normal\_bolus\_rate$ 
    grd4:  $sd\_module = d \wedge sd\_flag = s \Rightarrow r = s\_r$ 
    grd9:  $ctime \in \mathbb{N}$ 
    grd5:  $ctime > sd\_now$ 
    grd10:  $t2 \in \mathbb{N}$ 
    grd6:  $sd\_module = s \Rightarrow t2 = ctime + d\_deliver\_time$ 
    grd7:  $sd\_module = d \wedge sd\_flag = d \Rightarrow t2 = ctime + d\_deliver\_time - s.t$ 
    grd8:  $sd\_module = d \wedge sd\_flag = s \Rightarrow t2 = ctime + d\_deliver\_time$ 
  then
    act1: state := deliver
    act4: d_deliver_rate := r
    act5: sd_now := ctime
    act6: sd_rate_c :=  $\lambda x \cdot x \in ctime .. t2$ |r

```

```
    act7: sd_new_now := t2
  end
Event update_to_dual ⟨ordinary⟩ ≐
extends update_to_dual
  any
    ctime
  where
    grd2: state = deliver
    grd3: sd_module = d
    grd4: sd_flag = d
    grd5: ctime = sd_new_now
  then
    act2: d_deliver_rate := s_r
    act3: sd_flag := s
    act4: sd_now := ctime
    act5: sd_new_now := ctime + s_t
    act6: sd_rate_c := λx·x ∈ ctime .. ctime + s_t | s_r
  end
END
```

MACHINE Square_Dual_bolus2_continuous_2**REFINES** Square_Dual_bolus2_continuous**SEES** c_sd_bolus,c_normalbolus**VARIABLES**

state
 s.r
 s.t
 d.deliver_time
 d.deliver_rate
 d.t
 sd.module
 sd.flag
 sd.now
 sd.new_now
 sd.rate.c
 time
 t.sd

INVARIANTS

inv1: $time \in \mathbb{N}$
inv3: $t.sd \in \mathbb{N}$
inv4: $state = preempt \Rightarrow t.sd \leq d.t + s.t$
inv5: $state = deliver \Rightarrow t.sd \leq time + d.t + s.t$
inv6: $state = deliver \Rightarrow t.sd \geq time$
inv8: $state = deliver \Rightarrow t.sd - time \leq d.deliver_time$
inv7: $state \in \{deliver\} \wedge sd.module = d \wedge sd.flag = s \Rightarrow sd.new_now = t.sd$
inv11: $state \in \{deliver\} \wedge sd.module = s \Rightarrow sd.new_now = t.sd$
inv2: *(theorem)* $state = deliver \Rightarrow t.sd - time \in 0 .. d.deliver_time$
inv9: $state \in \{deliver\} \wedge sd.module = d \wedge sd.flag = d \Rightarrow sd.new_now + s.t = t.sd$
inv10: $state = preempt \Rightarrow d.deliver_time = t.sd$
inv12: $state = deliver \wedge sd.module = d \wedge sd.flag = d \Rightarrow time \leq sd.new_now$

EVENTS**Initialisation** *(extended)***begin**

act1: $state := off$
act2: $s.r := 0$
act3: $s.t := 0$
act6: $d.deliver_time := 0$
act7: $d.deliver_rate := 0$
act8: $d.t := 0$
act9: $sd.module := s$
act10: $sd.flag := d$
act11: $sd.now := 0$
act12: $sd.new_now := 0$
act13: $sd.rate.c := \{0 \mapsto 0\}$
act14: $time := 0$
act15: $t.sd := 0$

end**Event** start *(ordinary)* $\hat{=}$ **refines** start**any**

t
 r

where**grd1:** $state = off$

```

    grd2:  $t \in \mathbb{N}_1$ 
    grd3:  $r \in \mathbb{N}_1$ 
    grd4:  $time \geq sd\_now$ 
with
    ctime:  $ctime = time$ 
then
    act1:  $state := deliver$ 
    act2:  $s\_r := r$ 
    act3:  $s\_t := t$ 
    act6:  $sd\_module := s$ 
    act7:  $d\_deliver\_time := t$ 
    act8:  $d\_deliver\_rate := r$ 
    act9:  $sd\_rate.c := \lambda x \cdot x \in time .. time + t | r$ 
    act10:  $sd\_now := time$ 
    act11:  $sd\_new\_now := time + t$ 
    act12:  $t\_sd := time + t$ 
end
Event start_dual  $\langle ordinary \rangle \hat{=}$ 
refines start_dual
any
    t
    r
    td
where
    grd1:  $state = off$ 
    grd2:  $t \in \mathbb{N}_1$ 
    grd3:  $r \in \mathbb{N}_1$ 
    grd4:  $td \in \mathbb{N}_1$ 
    grd5:  $time \geq sd\_now$ 
with
    ctime:  $ctime = time$ 
then
    act1:  $state := deliver$ 
    act2:  $s\_r := r$ 
    act3:  $s\_t := t$ 
    act6:  $d\_deliver\_time := t + td$ 
    act7:  $d\_deliver\_rate := normal\_bolus\_rate$ 
    act8:  $d\_t := td$ 
    act9:  $sd\_module := d$ 
    act11:  $sd\_rate.c := \lambda x \cdot x \in time .. time + td | normal\_bolus\_rate$ 
    act12:  $sd\_now := time$ 
    act10:  $sd\_new\_now := time + td$ 
    act13:  $t\_sd := time + t + td$ 
end
Event finish  $\langle ordinary \rangle \hat{=}$ 
refines finish
when
    grd1:  $state = deliver$ 
    grd2:  $sd\_module = d \Rightarrow sd\_flag = s$ 
    grd3:  $time = sd\_new\_now$ 
    grd4:  $\langle theorem \rangle time = t\_sd$ 
with
    ctime:  $ctime = time$ 
then
    act1:  $state := off$ 
    act4:  $s\_r := 0$ 
    act5:  $s\_t := 0$ 
    act6:  $d\_deliver\_time := 0$ 
    act7:  $d\_deliver\_rate := 0$ 

```

```

    act8:  $d.t := 0$ 
    act9:  $sd\_flag := d$ 
    act10:  $sd\_rate.c := \lambda x.x \geq time|0$ 
    act11:  $sd\_now := time$ 
  end
Event suspend ⟨ordinary⟩  $\hat{=}$ 
refines suspend
  when
    grd1:  $state = deliver$ 
    grd2:  $time \in sd\_now .. sd\_new\_now$ 
  with
    ctime:  $ctime = time$ 
  then
    act1:  $state := suspend$ 
    act4:  $s.r := 0$ 
    act5:  $s.t := 0$ 
    act6:  $d.deliver\_time := 0$ 
    act7:  $d.deliver\_rate := 0$ 
    act8:  $d.t := 0$ 
    act9:  $sd\_flag := d$ 
    act10:  $sd\_now := time$ 
    act11:  $sd\_rate.c := \lambda x.x \geq time|0$ 
  end
Event resume ⟨ordinary⟩  $\hat{=}$ 
refines resume
  when
    grd1:  $state = suspend$ 
    grd2:  $time > sd\_now$ 
  with
    ctime:  $ctime = time$ 
  then
    act1:  $state := off$ 
    act2:  $sd\_now := time$ 
    act3:  $sd\_rate.c := \lambda x.x \geq time|0$ 
  end
Event preempted ⟨ordinary⟩  $\hat{=}$ 
refines preempted
  when
    grd1:  $state = deliver$ 
    grd3:  $time \in sd\_now .. sd\_new\_now$ 
    grd4:  $sd\_module = d \wedge sd\_flag = d \Rightarrow t\_sd - time \in s.t + 1 .. d.deliver\_time$ 
    grd5:  $sd\_module = d \wedge sd\_flag = s \Rightarrow t\_sd - time \in 0 .. s.t$ 
  with
    ctime:  $ctime = time$ 
    t:  $t = t\_sd - time$ 
  then
    act1:  $state := preempt$ 
    act4:  $d.deliver\_time := t\_sd - time$ 
    act5:  $d.deliver\_rate := 0$ 
    act6:  $sd\_now := time$ 
    act7:  $sd\_rate.c := \lambda x.x \geq time|0$ 
    act8:  $t\_sd := t\_sd - time$ 
  end
Event resume_from_preempt ⟨ordinary⟩  $\hat{=}$ 
refines resume_from_preempt
  any
    r
    t2

```

```

where
  grd1: state = preempt
  grd2: sd_module = s ⇒ r = s_r
  grd3: sd_module = d ∧ sd_flag = d ⇒ r = normal_bolus_rate
  grd4: sd_module = d ∧ sd_flag = s ⇒ r = s_r
  grd5: time > sd_now
  grd6: sd_module = s ⇒ t2 = time + d_deliver_time
  grd7: sd_module = d ∧ sd_flag = d ⇒ t2 = time + d_deliver_time - s_t
  grd8: sd_module = d ∧ sd_flag = s ⇒ t2 = time + d_deliver_time
with
  ctime: ctime = time
then
  act1: state := deliver
  act4: d_deliver_rate := r
  act5: sd_now := time
  act6: sd_rate.c := λx.x ∈ time .. t2|r
  act7: sd_new_now := t2
  act8: t_sd := time + t_sd
end
Event update_to_dual ⟨ordinary⟩ ≐
refines update_to_dual
when
  grd2: state = deliver
  grd3: sd_module = d
  grd4: sd_flag = d
  grd5: time = sd_new_now
with
  ctime: ctime = time
then
  act2: d_deliver_rate := s_r
  act3: sd_flag := s
  act4: sd_now := time
  act5: sd_new_now := time + s_t
  act6: sd_rate.c := λx.x ∈ time .. time + s_t|s_r
end
Event timer ⟨ordinary⟩ ≐
when
  grd1:
    ¬((state = deliver ∧ (sd_module = d ⇒ sd_flag = s) ∧ time = sd_new_now ∧ time = t_sd) ∨
      (state = deliver ∧ sd_module = d ∧ sd_flag = d ∧ time = sd_new_now))
then
  act1: time := time + 1
end
END

```

MACHINE Basal**SEES** c_basal**VARIABLES**

rate_setting
 basal_rate_in
 basal_mode

INVARIANTS

inv1: $rate_setting \in 0..c-1 \mapsto 0..basal_max \wedge 0 \in dom(rate_setting)$
 inv2: $basal_rate_in \in 0..basal_max$
 inv3: $basal_mode \in BASALMODE$

EVENTS**Initialisation****begin**

act1: $rate_setting := \{0 \mapsto 0\}$
 act2: $basal_rate_in := 0$
 act3: $basal_mode := stop$

end**Event** basal_suspend $\langle ordinary \rangle \hat{=}$ **when**

grd1: $basal_rate_in \neq 0$
 grd2: $basal_mode = delivering$

then

act1: $basal_rate_in := 0$
 act2: $basal_mode := suspended$

end**Event** basal_resume $\langle ordinary \rangle \hat{=}$ **any**

t

where

grd1: $basal_rate_in = 0$
 grd2: $t \in 0..c-1$
 grd3: $basal_mode = suspended$

then

act1: $basal_rate_in := rate_setting(max(\{i | i \in dom(rate_setting) \wedge i \leq t\}))$
 act2: $basal_mode := delivering$

end**Event** change_setting $\langle ordinary \rangle \hat{=}$ **any**

t

r

where

grd1: $t \in dom(rate_setting)$
 grd2: $r \in 0..basal_max$

then

act1: $rate_setting := rate_setting \Leftarrow \{t \mapsto r\}$

end**Event** delete_setting $\langle ordinary \rangle \hat{=}$ **any**

t

where

grd1: $t \in dom(rate_setting) \setminus \{0\}$
 grd2: $basal_mode \neq suspended$

then

act1: $rate_setting := \{t\} \Leftarrow rate_setting$

end**Event** add_setting $\langle ordinary \rangle \hat{=}$

```

any
  t
  r
where
  grd1:  $t \notin \text{dom}(\text{rate\_setting})$ 
  grd5:  $t \in 0 .. c - 1$ 
  grd3:  $r \in 0 .. \text{basal\_max}$ 
  grd4:  $\text{basal\_mode} \neq \text{suspended}$ 
then
  act1:  $\text{rate\_setting} := \text{rate\_setting} \cup \{t \mapsto r\}$ 
end
Event rate_update ⟨ordinary⟩  $\hat{=}$ 
any
  t
where
  grd1:  $\text{basal\_mode} = \text{delivering}$ 
  grd2:  $t \in \text{dom}(\text{rate\_setting})$ 
then
  act1:  $\text{basal\_rate\_in} := \text{rate\_setting}(t)$ 
end
Event start ⟨ordinary⟩  $\hat{=}$ 
any
  t
where
  grd1:  $\text{basal\_mode} = \text{stop}$ 
  grd2:  $t \in 0 .. c - 1$ 
then
  act1:  $\text{basal\_mode} := \text{delivering}$ 
  act2:  $\text{basal\_rate\_in} := \text{rate\_setting}(\max(\{i \mid i \in \text{dom}(\text{rate\_setting}) \wedge i \leq t\}))$ 
end
Event stop ⟨ordinary⟩  $\hat{=}$ 
when
  grd1:  $\text{basal\_mode} = \text{delivering}$ 
then
  act1:  $\text{basal\_mode} := \text{stop}$ 
  act2:  $\text{basal\_rate\_in} := 0$ 
end
END

```


MACHINE Basal1**REFINES** Basal**SEES** c_basal**VARIABLES**

rate_setting
 basal_rate_in
 basal_mode
 btime

INVARIANTS

inv1: $btime \in 1 .. c$

EVENTS**Initialisation** ⟨extended⟩**begin**

act1: $rate_setting := \{0 \mapsto 0\}$
 act2: $basal_rate_in := 0$
 act3: $basal_mode := stop$
 act4: $btime := c$

end**Event** basal_suspend ⟨ordinary⟩ $\hat{=}$ **extends** basal_suspend**when**

grd1: $basal_rate_in \neq 0$
 grd2: $basal_mode = delivering$

then

act1: $basal_rate_in := 0$
 act2: $basal_mode := suspended$

end**Event** basal_resume ⟨ordinary⟩ $\hat{=}$ **extends** basal_resume**any**

t
 $t2$

where

grd1: $basal_rate_in = 0$
 grd2: $t \in 0 .. c - 1$
 grd3: $basal_mode = suspended$
 grd4: $\{i | i \in dom(rate_setting) \wedge i > t\} = \emptyset \Rightarrow t2 = c$
 grd5: $\{i | i \in dom(rate_setting) \wedge i > t\} \neq \emptyset \Rightarrow t2 = \min(\{i | i \in dom(rate_setting) \wedge i > t\})$

then

act1: $basal_rate_in := rate_setting(max(\{i | i \in dom(rate_setting) \wedge i \leq t\}))$
 act2: $basal_mode := delivering$
 act3: $btime := t2 - t$

end**Event** change_setting ⟨ordinary⟩ $\hat{=}$ **extends** change_setting**any**

t
 r

where

grd1: $t \in dom(rate_setting)$
 grd2: $r \in 0 .. basal_max$

then

act1: $rate_setting := rate_setting \Leftarrow \{t \mapsto r\}$

end**Event** delete_setting ⟨ordinary⟩ $\hat{=}$ **extends** delete_setting

```

any
  t
where
  grd1:  $t \in \text{dom}(\text{rate\_setting}) \setminus \{0\}$ 
  grd2:  $\text{basal\_mode} \neq \text{suspended}$ 
then
  act1:  $\text{rate\_setting} := \{t\} \triangleleft \text{rate\_setting}$ 
end
Event add_setting ⟨ordinary⟩  $\hat{=}$ 
extends add_setting
  any
    t
    r
  where
  grd1:  $t \notin \text{dom}(\text{rate\_setting})$ 
  grd5:  $t \in 0 .. c - 1$ 
  grd3:  $r \in 0 .. \text{basal\_max}$ 
  grd4:  $\text{basal\_mode} \neq \text{suspended}$ 
then
  act1:  $\text{rate\_setting} := \text{rate\_setting} \cup \{t \mapsto r\}$ 
end
Event rate_update ⟨ordinary⟩  $\hat{=}$ 
extends rate_update
  any
    t
    t2
  where
  grd1:  $\text{basal\_mode} = \text{delivering}$ 
  grd2:  $t \in \text{dom}(\text{rate\_setting})$ 
  grd3:  $\{i | i \in \text{dom}(\text{rate\_setting}) \wedge i > t\} = \emptyset \Rightarrow t2 = c$ 
  grd4:  $\{i | i \in \text{dom}(\text{rate\_setting}) \wedge i > t\} \neq \emptyset \Rightarrow t2 = \min(\{i | i \in \text{dom}(\text{rate\_setting}) \wedge i > t\})$ 
then
  act1:  $\text{basal\_rate\_in} := \text{rate\_setting}(t)$ 
  act2:  $\text{btime} := t2 - t$ 
end
Event start ⟨ordinary⟩  $\hat{=}$ 
extends start
  any
    t
    t2
  where
  grd1:  $\text{basal\_mode} = \text{stop}$ 
  grd2:  $t \in 0 .. c - 1$ 
  grd3:  $\{i | i \in \text{dom}(\text{rate\_setting}) \wedge i > t\} = \emptyset \Rightarrow t2 = c$ 
  grd4:  $\{i | i \in \text{dom}(\text{rate\_setting}) \wedge i > t\} \neq \emptyset \Rightarrow t2 = \min(\{i | i \in \text{dom}(\text{rate\_setting}) \wedge i > t\})$ 
then
  act1:  $\text{basal\_mode} := \text{delivering}$ 
  act2:  $\text{basal\_rate\_in} := \text{rate\_setting}(\max(\{i | i \in \text{dom}(\text{rate\_setting}) \wedge i \leq t\}))$ 
  act3:  $\text{btime} := t2 - t$ 
end
Event stop ⟨ordinary⟩  $\hat{=}$ 
extends stop
  when
  grd1:  $\text{basal\_mode} = \text{delivering}$ 
  then
  act1:  $\text{basal\_mode} := \text{stop}$ 
  act2:  $\text{basal\_rate\_in} := 0$ 
end
END

```

MACHINE Basal2**REFINES** Basal1**SEES** c_basal**VARIABLES**

rate_setting
 basal_rate_in
 basal_mode
 btime
 rate_setting2

INVARIANTS

inv1: $rate_setting2 \in 0..c-1 \rightarrow 0..basal_max \cup \{-1\}$
inv2: $rate_setting \subseteq rate_setting2$
inv3: $rate_setting2 \triangleright \{-1\} = rate_setting$
inv4: $\langle \text{theorem} \rangle \forall t \cdot t \in 0..c-1 \Rightarrow ((\forall j \cdot j \in dom(rate_setting2) \wedge j > t \Rightarrow rate_setting2(j) = -1) \Leftrightarrow \{i | i \in dom(rate_setting) \wedge i > t\} = \emptyset)$

EVENTS**Initialisation** $\langle \text{extended} \rangle$ **begin**

act1: $rate_setting := \{0 \mapsto 0\}$
act2: $basal_rate_in := 0$
act3: $basal_mode := stop$
act4: $btime := c$
act5: $rate_setting2 := (1..c-1 \times \{-1\}) \cup \{0 \mapsto 0\}$

end**Event** basal_suspend $\langle \text{ordinary} \rangle \hat{=}$ **extends** basal_suspend**when**

grd1: $basal_rate_in \neq 0$
grd2: $basal_mode = delivering$

then

act1: $basal_rate_in := 0$
act2: $basal_mode := suspended$

end**Event** basal_resume $\langle \text{ordinary} \rangle \hat{=}$ **refines** basal_resume**any**

t
 t2

where

grd1: $basal_rate_in = 0$
grd2: $t \in 0..c-1$
grd3: $basal_mode = suspended$
grd6: $(\forall j \cdot j \in dom(rate_setting2) \wedge j > t \Rightarrow rate_setting2(j) = -1) \Rightarrow t2 = c$
grd7: $(\exists j \cdot j \in dom(rate_setting2) \wedge j > t \wedge rate_setting2(j) \neq -1) \Rightarrow t2 = \min(\{i | i \in dom(rate_setting2) \wedge i > t\})$
grd8: $\langle \text{theorem} \rangle (\forall j \cdot j \in dom(rate_setting2) \wedge j > t \Rightarrow rate_setting2(j) = -1) \Leftrightarrow \{i | i \in dom(rate_setting) \wedge i > t\} = \emptyset$
grd9: $\langle \text{theorem} \rangle (\exists j \cdot j \in dom(rate_setting2) \wedge j > t \wedge rate_setting2(j) \neq -1) \Leftrightarrow \{i | i \in dom(rate_setting) \wedge i > t\} \neq \emptyset$
grd4: $\langle \text{theorem} \rangle \{i | i \in dom(rate_setting) \wedge i > t\} = \emptyset \Rightarrow t2 = c$
grd5: $\langle \text{theorem} \rangle \{i | i \in dom(rate_setting) \wedge i > t\} \neq \emptyset \Rightarrow t2 = \min(\{i | i \in dom(rate_setting) \wedge i > t\})$

then

act1: $basal_rate_in := rate_setting2(\max(\{i | i \in dom(rate_setting2) \wedge i \leq t\}))$
act2: $basal_mode := delivering$
act3: $btime := t2 - t$

end

Event change_setting ⟨ordinary⟩ $\hat{=}$

refines change_setting

any

t

r

where

grd1: $t \in \text{dom}(\text{rate_setting2} \triangleright \{-1\})$

grd2: $r \in 0 .. \text{basal_max}$

then

act1: $\text{rate_setting} := \text{rate_setting} \triangleleft \{t \mapsto r\}$

act2: $\text{rate_setting2} := \text{rate_setting2} \triangleleft \{t \mapsto r\}$

end

Event delete_setting ⟨ordinary⟩ $\hat{=}$

refines delete_setting

any

t

where

grd1: $t \in \text{dom}(\text{rate_setting2} \triangleright \{-1\}) \setminus \{0\}$

grd2: $\text{basal_mode} \neq \text{suspended}$

then

act1: $\text{rate_setting} := \{t\} \triangleleft \text{rate_setting}$

act2: $\text{rate_setting2} := \text{rate_setting2} \triangleleft \{t \mapsto -1\}$

end

Event add_setting ⟨ordinary⟩ $\hat{=}$

refines add_setting

any

t

r

where

grd3: $r \in 0 .. \text{basal_max}$

grd4: $\text{basal_mode} \neq \text{suspended}$

grd5: $t \in 0 .. c - 1$

grd6: $\text{rate_setting2}(t) = -1$

grd1: ⟨theorem⟩ $t \notin \text{dom}(\text{rate_setting})$

then

act1: $\text{rate_setting} := \text{rate_setting} \cup \{t \mapsto r\}$

act2: $\text{rate_setting2} := \text{rate_setting2} \triangleleft \{t \mapsto r\}$

end

Event rate_update ⟨ordinary⟩ $\hat{=}$

refines rate_update

any

t

t2

where

grd1: $\text{basal_mode} = \text{delivering}$

grd11: $t \in \text{dom}(\text{rate_setting2} \triangleright \{-1\})$

grd2: ⟨theorem⟩ $t \in \text{dom}(\text{rate_setting})$

grd6: $(\forall j. j \in \text{dom}(\text{rate_setting2}) \wedge j > t \Rightarrow \text{rate_setting2}(j) = -1) \Rightarrow t2 = c$

grd7: $(\exists j. j \in \text{dom}(\text{rate_setting2}) \wedge j > t \wedge \text{rate_setting2}(j) \neq -1) \Rightarrow t2 = \min(\{i | i \in \text{dom}(\text{rate_setting2}) \triangleright \{-1\} \wedge i > t\})$

grd9: ⟨theorem⟩ $(\exists j. j \in \text{dom}(\text{rate_setting2}) \wedge j > t \wedge \text{rate_setting2}(j) \neq -1) \Leftrightarrow \{i | i \in \text{dom}(\text{rate_setting}) \wedge i > t\} \neq \emptyset$

grd10: ⟨theorem⟩ $(\forall j. j \in \text{dom}(\text{rate_setting2}) \wedge j > t \Rightarrow \text{rate_setting2}(j) = -1) \Leftrightarrow \{i | i \in \text{dom}(\text{rate_setting}) \wedge i > t\} = \emptyset$

grd3: ⟨theorem⟩ $\{i | i \in \text{dom}(\text{rate_setting}) \wedge i > t\} = \emptyset \Rightarrow t2 = c$

grd4: ⟨theorem⟩ $\{i | i \in \text{dom}(\text{rate_setting}) \wedge i > t\} \neq \emptyset \Rightarrow t2 = \min(\{i | i \in \text{dom}(\text{rate_setting}) \wedge i > t\})$

then

act1: $\text{basal_rate_in} := \text{rate_setting2}(t)$

```

    act2: btime := t2 - t
  end
Event start ⟨ordinary⟩ ≐
refines start
  any
    t
    t2
  where
    grd1: basal_mode = stop
    grd2: t ∈ 0 .. c - 1
    grd6: (∀j. j ∈ dom(rate_setting2) ∧ j > t ⇒ rate_setting2(j) = -1) ⇒ t2 = c
    grd7: (∃j. j ∈ dom(rate_setting2) ∧ j > t ∧ rate_setting2(j) ≠ -1) ⇒ t2 = min({i | i ∈ dom(rate_setting2) ⊃
      {-1} ∧ i > t})
    grd10: ⟨theorem⟩ (∀j. j ∈ dom(rate_setting2) ∧ j > t ⇒ rate_setting2(j) = -1) ⇔ {i | i ∈ dom(rate_setting) ∧
      i > t} = ∅
    grd9: ⟨theorem⟩ (∃j. j ∈ dom(rate_setting2) ∧ j > t ∧ rate_setting2(j) ≠ -1) ⇔ {i | i ∈ dom(rate_setting) ∧
      i > t} ≠ ∅
    grd3: ⟨theorem⟩ {i | i ∈ dom(rate_setting) ∧ i > t} = ∅ ⇒ t2 = c
    grd4: ⟨theorem⟩ {i | i ∈ dom(rate_setting) ∧ i > t} ≠ ∅ ⇒ t2 = min({i | i ∈ dom(rate_setting) ∧ i > t})
  then
    act1: basal_mode := delivering
    act2: basal_rate_in := rate_setting2(max({i | i ∈ dom(rate_setting2) ⊃ {-1} ∧ i ≤ t}))
    act3: btime := t2 - t
  end
Event stop ⟨ordinary⟩ ≐
extends stop
  when
    grd1: basal_mode = delivering
  then
    act1: basal_mode := stop
    act2: basal_rate_in := 0
  end
END

```

MACHINE Basal3**REFINES** Basal2**SEES** c_basal**VARIABLES**

basal_rate_in

basal_mode

btime

rate_setting2

EVENTS**Initialisation****begin**act2: *basal_rate_in* := 0act3: *basal_mode* := *stop*act4: *btime* := *c*act5: *rate_setting2* := $(1..c-1 \times \{-1\}) \cup \{0 \mapsto 0\}$ **end****Event** basal_suspend ⟨ordinary⟩ $\hat{=}$ **extends** basal_suspend**when**grd1: *basal_rate_in* \neq 0grd2: *basal_mode* = *delivering***then**act1: *basal_rate_in* := 0act2: *basal_mode* := *suspended***end****Event** basal_resume ⟨ordinary⟩ $\hat{=}$ **refines** basal_resume**any**

t

t2

wheregrd1: *basal_rate_in* = 0grd2: $t \in 0..c-1$ grd3: *basal_mode* = *suspended*grd6: $(\forall j. j \in \text{dom}(\text{rate_setting2}) \wedge j > t \Rightarrow \text{rate_setting2}(j) = -1) \Rightarrow t2 = c$ grd7: $(\exists j. j \in \text{dom}(\text{rate_setting2}) \wedge j > t \wedge \text{rate_setting2}(j) \neq -1) \Rightarrow t2 = \min(\{i | i \in \text{dom}(\text{rate_setting2}) \triangleright \{-1\} \wedge i > t\})$ **then**act1: *basal_rate_in* := *rate_setting2*($\max(\{i | i \in \text{dom}(\text{rate_setting2}) \triangleright \{-1\} \wedge i \leq t\})$)act2: *basal_mode* := *delivering*act3: *btime* := *t2* - *t***end****Event** change_setting ⟨ordinary⟩ $\hat{=}$ **refines** change_setting**any**

t

r

wheregrd1: $t \in \text{dom}(\text{rate_setting2}) \triangleright \{-1\}$ grd2: $r \in 0..basal_max$ **then**act2: *rate_setting2* := *rate_setting2* \triangleleft $\{t \mapsto r\}$ **end****Event** delete_setting ⟨ordinary⟩ $\hat{=}$ **refines** delete_setting**any**

```

    t
  where
    grd1:  $t \in \text{dom}(\text{rate\_setting2} \triangleright \{-1\}) \setminus \{0\}$ 
    grd2:  $\text{basal\_mode} \neq \text{suspended}$ 
  then
    act2:  $\text{rate\_setting2} := \text{rate\_setting2} \triangleleft \{t \mapsto -1\}$ 
  end
Event add_setting ⟨ordinary⟩  $\hat{=}$ 
refines add_setting
  any
    t
    r
  where
    grd3:  $r \in 0 .. \text{basal\_max}$ 
    grd4:  $\text{basal\_mode} \neq \text{suspended}$ 
    grd5:  $t \in 0 .. c - 1$ 
    grd6:  $\text{rate\_setting2}(t) = -1$ 
  then
    act2:  $\text{rate\_setting2} := \text{rate\_setting2} \triangleleft \{t \mapsto r\}$ 
  end
Event rate_update ⟨ordinary⟩  $\hat{=}$ 
refines rate_update
  any
    t
    t2
  where
    grd1:  $\text{basal\_mode} = \text{delivering}$ 
    grd11:  $t \in \text{dom}(\text{rate\_setting2} \triangleright \{-1\})$ 
    grd6:  $(\forall j. j \in \text{dom}(\text{rate\_setting2}) \wedge j > t \Rightarrow \text{rate\_setting2}(j) = -1) \Rightarrow t2 = c$ 
    grd7:  $(\exists j. j \in \text{dom}(\text{rate\_setting2}) \wedge j > t \wedge \text{rate\_setting2}(j) \neq -1) \Rightarrow t2 = \min(\{i | i \in \text{dom}(\text{rate\_setting2} \triangleright \{-1\}) \wedge i > t\})$ 
  then
    act1:  $\text{basal\_rate\_in} := \text{rate\_setting2}(t)$ 
    act2:  $\text{btime} := t2 - t$ 
  end
Event start ⟨ordinary⟩  $\hat{=}$ 
refines start
  any
    t
    t2
  where
    grd1:  $\text{basal\_mode} = \text{stop}$ 
    grd2:  $t \in 0 .. c - 1$ 
    grd6:  $(\forall j. j \in \text{dom}(\text{rate\_setting2}) \wedge j > t \Rightarrow \text{rate\_setting2}(j) = -1) \Rightarrow t2 = c$ 
    grd7:  $(\exists j. j \in \text{dom}(\text{rate\_setting2}) \wedge j > t \wedge \text{rate\_setting2}(j) \neq -1) \Rightarrow t2 = \min(\{i | i \in \text{dom}(\text{rate\_setting2} \triangleright \{-1\}) \wedge i > t\})$ 
  then
    act1:  $\text{basal\_mode} := \text{delivering}$ 
    act2:  $\text{basal\_rate\_in} := \text{rate\_setting2}(\max(\{i | i \in \text{dom}(\text{rate\_setting2} \triangleright \{-1\}) \wedge i \leq t\}))$ 
    act3:  $\text{btime} := t2 - t$ 
  end
Event stop ⟨ordinary⟩  $\hat{=}$ 
extends stop
  when
    grd1:  $\text{basal\_mode} = \text{delivering}$ 
  then
    act1:  $\text{basal\_mode} := \text{stop}$ 
    act2:  $\text{basal\_rate\_in} := 0$ 
  end
END

```

MACHINE Basal4**REFINES** Basal3**SEES** c_basal**VARIABLES**

basal_rate_in
 basal_mode
 btime
 rate_setting2
 min_value
 max_value

INVARIANTS

inv1: $min_value \in 0..c$
inv2: $max_value \in 0..basal_max$

EVENTS**Initialisation** ⟨extended⟩**begin**

act2: $basal_rate_in := 0$
act3: $basal_mode := stop$
act4: $btime := c$
act5: $rate_setting2 := (1..c-1 \times \{-1\}) \cup \{0 \mapsto 0\}$
act6: $min_value := 0$
act7: $max_value := 0$

end**Event** basal_suspend ⟨ordinary⟩ $\hat{=}$ **extends** basal_suspend**when**

grd1: $basal_rate_in \neq 0$
grd2: $basal_mode = delivering$

then

act1: $basal_rate_in := 0$
act2: $basal_mode := suspended$

end**Event** basal_resume ⟨ordinary⟩ $\hat{=}$ **extends** basal_resume**any**

t
t2

where

grd1: $basal_rate_in = 0$
grd2: $t \in 0..c-1$
grd3: $basal_mode = suspended$
grd6: $(\forall j. j \in dom(rate_setting2) \wedge j > t \Rightarrow rate_setting2(j) = -1) \Rightarrow t2 = c$
grd7: $(\exists j. j \in dom(rate_setting2) \wedge j > t \wedge rate_setting2(j) \neq -1) \Rightarrow t2 = min(\{i | i \in dom(rate_setting2) \triangleright \{-1\} \wedge i > t\})$

then

act1: $basal_rate_in := rate_setting2(max(\{i | i \in dom(rate_setting2) \triangleright \{-1\} \wedge i \leq t\}))$
act2: $basal_mode := delivering$
act3: $btime := t2 - t$

end**Event** change_setting ⟨ordinary⟩ $\hat{=}$ **extends** change_setting**any**

t
r

where

grd1: $t \in dom(rate_setting2) \triangleright \{-1\}$


```

    grd2:  $r \in 0 .. basal\_max$ 
  then
    act2:  $rate\_setting2 := rate\_setting2 \triangleleft \{t \mapsto r\}$ 
  end
Event delete_setting ⟨ordinary⟩  $\hat{=}$ 
extends delete_setting
  any
     $t$ 
  where
    grd1:  $t \in dom(rate\_setting2 \triangleright \{-1\}) \setminus \{0\}$ 
    grd2:  $basal\_mode \neq suspended$ 
  then
    act2:  $rate\_setting2 := rate\_setting2 \triangleleft \{t \mapsto -1\}$ 
  end
Event add_setting ⟨ordinary⟩  $\hat{=}$ 
extends add_setting
  any
     $t$ 
     $r$ 
  where
    grd3:  $r \in 0 .. basal\_max$ 
    grd4:  $basal\_mode \neq suspended$ 
    grd5:  $t \in 0 .. c - 1$ 
    grd6:  $rate\_setting2(t) = -1$ 
  then
    act2:  $rate\_setting2 := rate\_setting2 \triangleleft \{t \mapsto r\}$ 
  end
Event rate_update ⟨ordinary⟩  $\hat{=}$ 
extends rate_update
  any
     $t$ 
     $t2$ 
  where
    grd1:  $basal\_mode = delivering$ 
    grd11:  $t \in dom(rate\_setting2 \triangleright \{-1\})$ 
    grd6:  $(\forall j. j \in dom(rate\_setting2) \wedge j > t \Rightarrow rate\_setting2(j) = -1) \Rightarrow t2 = c$ 
    grd7:  $(\exists j. j \in dom(rate\_setting2) \wedge j > t \wedge rate\_setting2(j) \neq -1) \Rightarrow t2 = min(\{i | i \in dom(rate\_setting2) \triangleright \{-1\} \wedge i > t\})$ 
  then
    act1:  $basal\_rate\_in := rate\_setting2(t)$ 
    act2:  $btime := t2 - t$ 
  end
Event start ⟨ordinary⟩  $\hat{=}$ 
extends start
  any
     $t$ 
     $t2$ 
  where
    grd1:  $basal\_mode = stop$ 
    grd2:  $t \in 0 .. c - 1$ 
    grd6:  $(\forall j. j \in dom(rate\_setting2) \wedge j > t \Rightarrow rate\_setting2(j) = -1) \Rightarrow t2 = c$ 
    grd7:  $(\exists j. j \in dom(rate\_setting2) \wedge j > t \wedge rate\_setting2(j) \neq -1) \Rightarrow t2 = min(\{i | i \in dom(rate\_setting2) \triangleright \{-1\} \wedge i > t\})$ 
  then
    act1:  $basal\_mode := delivering$ 
    act2:  $basal\_rate\_in := rate\_setting2(max(\{i | i \in dom(rate\_setting2) \triangleright \{-1\} \wedge i \leq t\}))$ 
    act3:  $btime := t2 - t$ 
  end

```

```

Event stop ⟨ordinary⟩ ≐
extends stop
  when
    grd1: basal_mode = delivering
  then
    act1: basal_mode := stop
    act2: basal_rate.in := 0
  end
Event get_min_value_1 ⟨ordinary⟩ ≐
  any
    t
  where
    grd5:  $t \in 0..c-1$ 
    grd3:  $\forall j \cdot j \in \text{dom}(\text{rate\_setting2}) \wedge j > t \Rightarrow \text{rate\_setting2}(j) = -1$ 
  then
    act1: min_value := c
  end
Event get_min_value_2 ⟨ordinary⟩ ≐
  any
    t
  where
    grd5:  $t \in 0..c-1$ 
    grd4:  $\exists j \cdot j \in \text{dom}(\text{rate\_setting2}) \wedge j > t \wedge \text{rate\_setting2}(j) \neq -1$ 
  then
    act1: min_value := min({i | i ∈ dom(rate_setting2 ⊃ {-1}) ∧ i > t})
  end
Event get_max_value ⟨ordinary⟩ ≐
  any
    t
  where
    grd1:  $t \in 0..c-1$ 
  then
    act1: max_value := rate_setting2(max({i | i ∈ dom(rate_setting2 ⊃ {-1}) ∧ i ≤ t})
  end
END

```

MACHINE Basal5**REFINES** Basal4**SEES** c_basal**VARIABLES**

basal_rate_in
 basal_mode
 btime
 rate_setting2
 min_value
 get_min_value_add
 par_t
 temp_min
 get_min_start_t
 max_value
 get_max_start_t
 get_max_value_add
 par_t_max

INVARIANTS

inv1: $get_min_value_add \in 0..3$
inv2: $par_t \in \mathbb{N}$
inv3: $temp_min \in 0..c$
inv4: $get_min_start_t \in 0..c-1$
inv7: $get_min_value_add = 3 \Rightarrow \{i | i \in dom(rate_setting2 \triangleright \{-1\}) \wedge i > get_min_start_t\} \neq \emptyset$
inv5: $get_min_value_add = 3 \Rightarrow temp_min = min(\{i | i \in dom(rate_setting2 \triangleright \{-1\}) \wedge i > get_min_start_t\})$

inv8: $get_min_value_add = 1 \Rightarrow par_t = get_min_start_t + 1$
inv10: $get_min_value_add = 2 \Rightarrow par_t > get_min_start_t$
inv9: $get_min_value_add = 2 \Rightarrow \{i | i \in dom(rate_setting2 \triangleright \{-1\}) \wedge i > get_min_start_t \wedge i \leq par_t - 1\} = \emptyset$
inv11: $get_max_start_t \in 0..c-1$
inv12: $get_max_value_add \in 0..2$
inv13: $par_t_max \in 0..c-1$
inv14: $get_max_value_add \in \{1, 2\} \Rightarrow get_max_start_t \in 0..c-1$
inv15: $get_max_value_add = 2 \Rightarrow par_t_max = max(\{i | i \in dom(rate_setting2 \triangleright \{-1\}) \wedge i \leq get_max_start_t\})$

inv16: $get_max_value_add = 1 \Rightarrow \{i | i \in dom(rate_setting2 \triangleright \{-1\}) \wedge i \leq get_max_start_t \wedge i \geq par_t_max + 1\} = \emptyset$
inv17: $get_max_value_add \in \{1, 2\} \Rightarrow par_t_max \leq get_max_start_t$

EVENTS**Initialisation** (extended)**begin**

act2: $basal_rate_in := 0$
act3: $basal_mode := stop$
act4: $btime := c$
act5: $rate_setting2 := (1..c-1 \times \{-1\}) \cup \{0 \mapsto 0\}$
act6: $min_value := 0$
act7: $max_value := 0$
act11: $get_min_value_add := 0$
act8: $par_t := 0$
act9: $temp_min := 0$
act10: $get_min_start_t := 0$
act12: $get_max_start_t := 0$
act13: $get_max_value_add := 0$
act14: $par_t_max := 0$

```

end
Event basal_suspend ⟨ordinary⟩ ≐
extends basal_suspend
when
  grd1: basal_rate_in ≠ 0
  grd2: basal_mode = delivering
then
  act1: basal_rate_in := 0
  act2: basal_mode := suspended
end
Event basal_resume ⟨ordinary⟩ ≐
extends basal_resume
any
  t
  t2
where
  grd1: basal_rate_in = 0
  grd2: t ∈ 0 .. c - 1
  grd3: basal_mode = suspended
  grd6: (∀j. j ∈ dom(rate_setting2) ∧ j > t ⇒ rate_setting2(j) = -1) ⇒ t2 = c
  grd7: (∃j. j ∈ dom(rate_setting2) ∧ j > t ∧ rate_setting2(j) ≠ -1) ⇒ t2 = min({i | i ∈ dom(rate_setting2) ▷
    {-1} ∧ i > t})
then
  act1: basal_rate_in := rate_setting2(max({i | i ∈ dom(rate_setting2) ▷ {-1} ∧ i ≤ t}))
  act2: basal_mode := delivering
  act3: btime := t2 - t
end
Event change_setting ⟨ordinary⟩ ≐
extends change_setting
any
  t
  r
where
  grd1: t ∈ dom(rate_setting2 ▷ {-1})
  grd2: r ∈ 0 .. basal_max
  grd3: get_min_value_add = 0
  grd4: get_max_value_add = 0
then
  act2: rate_setting2 := rate_setting2 ◁ {t ↦ r}
end
Event delete_setting ⟨ordinary⟩ ≐
extends delete_setting
any
  t
where
  grd1: t ∈ dom(rate_setting2 ▷ {-1}) \ {0}
  grd2: basal_mode ≠ suspended
  grd3: get_min_value_add = 0
  grd4: get_max_value_add = 0
then
  act2: rate_setting2 := rate_setting2 ◁ {t ↦ -1}
end
Event add_setting ⟨ordinary⟩ ≐
extends add_setting
any
  t
  r

```

```

where
  grd3:  $r \in 0 .. basal\_max$ 
  grd4:  $basal\_mode \neq suspended$ 
  grd5:  $t \in 0 .. c - 1$ 
  grd6:  $rate\_setting2(t) = -1$ 
  grd7:  $get\_min\_value\_add = 0$ 
  grd8:  $get\_max\_value\_add = 0$ 
then
  act2:  $rate\_setting2 := rate\_setting2 \Leftarrow \{t \mapsto r\}$ 
end
Event rate_update ⟨ordinary⟩  $\hat{=}$ 
extends rate_update
any
   $t$ 
   $t2$ 
where
  grd1:  $basal\_mode = delivering$ 
  grd11:  $t \in dom(rate\_setting2 \triangleright \{-1\})$ 
  grd6:  $(\forall j. j \in dom(rate\_setting2) \wedge j > t \Rightarrow rate\_setting2(j) = -1) \Rightarrow t2 = c$ 
  grd7:  $(\exists j. j \in dom(rate\_setting2) \wedge j > t \wedge rate\_setting2(j) \neq -1) \Rightarrow t2 = \min(\{i | i \in dom(rate\_setting2) \triangleright \{-1\} \wedge i > t\})$ 
then
  act1:  $basal\_rate\_in := rate\_setting2(t)$ 
  act2:  $btime := t2 - t$ 
end
Event start ⟨ordinary⟩  $\hat{=}$ 
extends start
any
   $t$ 
   $t2$ 
where
  grd1:  $basal\_mode = stop$ 
  grd2:  $t \in 0 .. c - 1$ 
  grd6:  $(\forall j. j \in dom(rate\_setting2) \wedge j > t \Rightarrow rate\_setting2(j) = -1) \Rightarrow t2 = c$ 
  grd7:  $(\exists j. j \in dom(rate\_setting2) \wedge j > t \wedge rate\_setting2(j) \neq -1) \Rightarrow t2 = \min(\{i | i \in dom(rate\_setting2) \triangleright \{-1\} \wedge i > t\})$ 
then
  act1:  $basal\_mode := delivering$ 
  act2:  $basal\_rate\_in := rate\_setting2(\max(\{i | i \in dom(rate\_setting2 \triangleright \{-1\}) \wedge i \leq t\}))$ 
  act3:  $btime := t2 - t$ 
end
Event stop ⟨ordinary⟩  $\hat{=}$ 
extends stop
when
  grd1:  $basal\_mode = delivering$ 
then
  act1:  $basal\_mode := stop$ 
  act2:  $basal\_rate\_in := 0$ 
end
Event get_min_value_1 ⟨ordinary⟩  $\hat{=}$ 
refines get_min_value_1
when
  grd4:  $get\_min\_value\_add = 2$ 
  grd5:  $par\_t = c$ 
  grd3: ⟨theorem⟩  $\forall j. j \in dom(rate\_setting2) \wedge j > get\_min\_start\_t \Rightarrow rate\_setting2(j) = -1$ 
with
   $t: t = get\_min\_start\_t$ 
then

```

```

    act1: min_value := c
    act2: get_min_value_add := 0
  end
Event get_min_value_2 ⟨ordinary⟩ ≐
refines get_min_value_2
  when
    grd5: get_min_value_add = 3
    grd4: ⟨theorem⟩  $\exists j. j \in \text{dom}(\text{rate\_setting2}) \wedge j > \text{get\_min\_start\_t} \wedge \text{rate\_setting2}(j) \neq -1$ 
  with
    t: t = get_min_start_t
  then
    act1: min_value := temp_min
    act2: get_min_value_add := 0
  end
Event get_min_value_start ⟨ordinary⟩ ≐
  any
    t
  where
    grd1: t ∈ 0 .. c - 1
    grd2: get_min_value_add = 0
  then
    act1: par_t := t + 1
    act2: get_min_value_add := 1
    act3: get_min_start_t := t
  end
Event find_min_value ⟨ordinary⟩ ≐
  when
    grd1: par_t < c
    grd2: get_min_value_add ∈ {1, 2}
    grd3: rate_setting2(par_t) = -1
  then
    act1: par_t := par_t + 1
    act2: get_min_value_add := 2
  end
Event find_min_value_2 ⟨ordinary⟩ ≐
  when
    grd1: par_t < c
    grd2: get_min_value_add ∈ {1, 2}
    grd3: rate_setting2(par_t) ≠ -1
  then
    act1: temp_min := par_t
    act2: get_min_value_add := 3
  end
Event get_max_value ⟨ordinary⟩ ≐
refines get_max_value
  when
    grd2: get_max_value_add = 2
  with
    t: t = get_max_start_t
  then
    act1: max_value := rate_setting2(par_t_max)
    act2: get_max_value_add := 0
  end
Event get_max_value_start ⟨ordinary⟩ ≐
  any
    t
  where
    grd1: t ∈ 0 .. c - 1

```

```
    grd2: get_max_value_add = 0
  then
    act1: get_max_start_t := t
    act2: get_max_value_add := 1
    act3: par_t_max := t
  end
Event get_max_value.1 ⟨ordinary⟩ ≐
  when
    grd1: get_max_value_add = 1
    grd3: par_t_max ≥ 0
    grd2: rate_setting2(par_t_max) = -1
  then
    act1: par_t_max := par_t_max - 1
  end
Event get_max_value.2 ⟨ordinary⟩ ≐
  when
    grd1: get_max_value_add = 1
    grd2: ⟨theorem⟩ par_t_max ≥ 0
    grd3: rate_setting2(par_t_max) ≠ -1
  then
    act1: get_max_value_add := 2
  end
END
```

MACHINE Basal6**REFINES** Basal5**SEES** c_basal2**VARIABLES**

basal_rate_in
 basal_mode
 btime
 rate_setting2
 min_value
 get_min_value_add
 par_t
 temp_min
 get_min_start_t
 max_value
 get_max_start_t
 get_max_value_add
 par_t_max
 prog_basal
 par_get_t
 add_resume
 add_update
 add_start

INVARIANTS**inv1:** $prog_basal \in PROC_BASAL$ **inv2:** $prog_basal = null \Rightarrow get_max_value_add = 0 \wedge get_min_value_add = 0$ **inv3:** $par_get_t \in 0..c-1$ **inv13:** $add_resume \in 0..3$ **inv14:** $add_update \in 0..3$ **inv15:** $add_start \in 0..3$ **inv17:** $prog_basal = null \Rightarrow add_resume = 0 \wedge add_update = 0 \wedge add_start = 0$ **inv18:** $add_resume \neq 0 \Rightarrow add_update = 0 \wedge add_start = 0$ **inv26:** $add_start \neq 0 \Rightarrow add_update = 0 \wedge add_resume = 0$ **inv27:** $add_update \neq 0 \Rightarrow add_resume = 0 \wedge add_start = 0$ **inv11:** $get_max_value_add \neq 0 \Rightarrow prog_basal = call_get_max$ **inv12:** $get_min_value_add \neq 0 \Rightarrow prog_basal = call_get_min$ **inv7:** $prog_basal \in \{call_get_min, return_get_min, call_get_max, return_get_max\} \Rightarrow par_get_t \in 0..c-1$ **inv8:** $get_min_value_add \in \{1, 2, 3\} \vee prog_basal \in \{return_get_min, call_get_max, return_get_max\} \Rightarrow get_min_start_t = par_get_t$ **inv10:** $get_max_value_add \in \{1, 2\} \vee prog_basal = return_get_max \Rightarrow get_max_start_t = par_get_t$ **inv5:** $(add_resume = 1 \wedge prog_basal = return_get_min) \vee add_resume = 2$ \Rightarrow $((\forall j. j \in dom(rate_setting2) \wedge j > par_get_t \Rightarrow rate_setting2(j) = -1) \Rightarrow min_value = c)$ **inv6:** $(add_resume = 1 \wedge prog_basal = return_get_min) \vee add_resume = 2$ \Rightarrow $((\exists j. j \in dom(rate_setting2) \wedge j > par_get_t \wedge rate_setting2(j) \neq -1) \Rightarrow min_value = min(\{i | i \in dom(rate_setting2) \triangleright \{-1\} \wedge i > par_get_t\}))$ **inv9:** $prog_basal = return_get_max \Rightarrow$ $max_value = rate_setting2(max(\{i | i \in dom(rate_setting2) \triangleright \{-1\} \wedge i \leq get_max_start_t\}))$ **inv16:** $add_update \in \{1, 2\} \Rightarrow par_get_t \in dom(rate_setting2) \triangleright \{-1\}$

inv20:
 $(add_start = 1 \wedge prog_basal = return_get_min) \vee add_start = 2$
 \Rightarrow
 $((\forall j. j \in dom(rate_setting2) \wedge j > par_get_t \Rightarrow rate_setting2(j) = -1) \Rightarrow min_value = c)$

inv19:
 $(add_start = 1 \wedge prog_basal = return_get_min) \vee add_start = 2$
 \Rightarrow
 $((\exists j. j \in dom(rate_setting2) \wedge j > par_get_t \wedge rate_setting2(j) \neq -1) \Rightarrow min_value = min(\{i | i \in dom(rate_setting2) \triangleright \{-1\} \wedge i > par_get_t\}))$

inv22:
 $add_update = 1 \wedge prog_basal = return_get_min$
 \Rightarrow
 $((\forall j. j \in dom(rate_setting2) \wedge j > par_get_t \Rightarrow rate_setting2(j) = -1) \Rightarrow min_value = c)$

inv21:
 $add_update = 1 \wedge prog_basal = return_get_min$
 \Rightarrow
 $((\exists j. j \in dom(rate_setting2) \wedge j > par_get_t \wedge rate_setting2(j) \neq -1) \Rightarrow min_value = min(\{i | i \in dom(rate_setting2) \triangleright \{-1\} \wedge i > par_get_t\}))$

inv23: $add_resume \in \{1, 2\} \Rightarrow basal_rate_in = 0 \wedge basal_mode = suspended$
inv24: $add_update = 1 \Rightarrow basal_mode = delivering \wedge prog_basal \in \{call_get_min, return_get_min\}$
inv25: $add_start \in \{1, 2\} \Rightarrow basal_mode = stop$

EVENTS

Initialisation (extended)

begin

act2: $basal_rate_in := 0$
act3: $basal_mode := stop$
act4: $btime := c$
act5: $rate_setting2 := (1..c - 1 \times \{-1\}) \cup \{0 \mapsto 0\}$
act6: $min_value := 0$
act7: $max_value := 0$
act11: $get_min_value_add := 0$
act8: $par_t := 0$
act9: $temp_min := 0$
act10: $get_min_start_t := 0$
act12: $get_max_start_t := 0$
act13: $get_max_value_add := 0$
act14: $par_t_max := 0$
act15: $prog_basal := null$
act16: $par_get_t := 0$
act17: $add_resume := 0$
act18: $add_update := 0$
act19: $add_start := 0$

end

Event basal_suspend (ordinary) $\hat{=}$

extends basal_suspend

when

grd1: $basal_rate_in \neq 0$
grd2: $basal_mode = delivering$
grd3: $prog_basal = null$

then

act1: $basal_rate_in := 0$
act2: $basal_mode := suspended$

end

Event change_setting (ordinary) $\hat{=}$

refines change_setting

any

t

```

    r
  where
    grd5: prog_basal = null
    grd6: t ∈ 0 .. c - 1
    grd7: rate_setting2(t) ≠ - 1
    grd2: r ∈ 0 .. basal_max
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ r}
  end
Event delete_setting ⟨ordinary⟩ ≐
refines delete_setting
  any
    t
  where
    grd5: prog_basal = null
    grd2: basal_mode ≠ suspended
    grd6: t ∈ 1 .. c - 1
    grd7: rate_setting2(t) ≠ - 1
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ - 1}
  end
Event add_setting ⟨ordinary⟩ ≐
refines add_setting
  any
    t
    r
  where
    grd9: prog_basal = null
    grd3: r ∈ 0 .. basal_max
    grd4: basal_mode ≠ suspended
    grd5: t ∈ 0 .. c - 1
    grd6: rate_setting2(t) = - 1
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ r}
  end
Event basal_resume_return ⟨ordinary⟩ ≐
refines basal_resume
  when
    grd8: prog_basal = return_get_max
    grd9: add_resume = 2
  with
    t2: t2 = min_value
    t: t = par_get_t
  then
    act1: basal_rate_in := max_value
    act2: basal_mode := delivering
    act3: btime := min_value - par_get_t
    act4: prog_basal := null
    act5: add_resume := 0
  end
Event basal_resume_call ⟨ordinary⟩ ≐
  any
    t
  where
    grd4: t ∈ 0 .. c - 1
    grd5: prog_basal = null
    grd6: add_resume = 0
    grd1: basal_rate_in = 0

```

```

    grd3: basal_mode = suspended
  then
    act1: par_get.t := t
    act2: prog_basal := call_get_min
    act3: add_resume := 1
  end
Event basal_resume_call_2 ⟨ordinary⟩ ≐
  when
    grd1: prog_basal = return_get_min
    grd2: add_resume = 1
  then
    act1: prog_basal := call_get_max
    act2: add_resume := 2
  end
Event rate_update_return ⟨ordinary⟩ ≐
refines rate_update
  when
    grd12: add_update = 1
    grd4: prog_basal = return_get_min
  with
    t2: t2 = min_value
    t: t = par_get.t
  then
    act1: basal_rate.in := rate_setting2(par_get.t)
    act2: btime := min_value - par_get.t
    act3: add_update := 0
    act4: prog_basal := null
  end
Event rate_update_call ⟨ordinary⟩ ≐
  any
    t
  where
    grd6: t ∈ 0 .. c - 1
    grd2: prog_basal = null
    grd3: add_update = 0
    grd5: basal_mode = delivering
    grd7: rate_setting2(t) ≠ -1
  then
    act1: par_get.t := t
    act2: prog_basal := call_get_min
    act3: add_update := 1
  end
Event start_return ⟨ordinary⟩ ≐
refines start
  when
    grd8: add_start = 2
    grd9: prog_basal = return_get_max
  with
    t2: t2 = min_value
    t: t = par_get.t
  then
    act1: basal_mode := delivering
    act2: basal_rate.in := max_value
    act3: btime := min_value - par_get.t
    act4: add_start := 0
    act5: prog_basal := null
  end
Event start_call ⟨ordinary⟩ ≐

```

```

any
  t
where
  grd1:  $t \in 0 .. c - 1$ 
  grd2:  $prog\_basal = null$ 
  grd3:  $add\_start = 0$ 
  grd4:  $basal\_mode = stop$ 
then
  act1:  $par\_get\_t := t$ 
  act2:  $prog\_basal := call\_get\_min$ 
  act3:  $add\_start := 1$ 
end
Event start_call_2 (ordinary)  $\hat{=}$ 
when
  grd1:  $prog\_basal = return\_get\_min$ 
  grd2:  $add\_start = 1$ 
then
  act1:  $prog\_basal := call\_get\_max$ 
  act2:  $add\_start := 2$ 
end
Event stop (ordinary)  $\hat{=}$ 
extends stop
when
  grd1:  $basal\_mode = delivering$ 
  grd2:  $prog\_basal = null$ 
then
  act1:  $basal\_mode := stop$ 
  act2:  $basal\_rate\_in := 0$ 
end
Event get_min_value_1 (ordinary)  $\hat{=}$ 
refines get_min_value_1
when
  grd4:  $get\_min\_value\_add = 2$ 
  grd5:  $par\_t = c$ 
then
  act1:  $min\_value := c$ 
  act2:  $get\_min\_value\_add := 0$ 
  act3:  $prog\_basal := return\_get\_min$ 
end
Event get_min_value_2 (ordinary)  $\hat{=}$ 
refines get_min_value_2
when
  grd5:  $get\_min\_value\_add = 3$ 
then
  act1:  $min\_value := temp\_min$ 
  act2:  $get\_min\_value\_add := 0$ 
  act3:  $prog\_basal := return\_get\_min$ 
end
Event get_min_value_start (ordinary)  $\hat{=}$ 
refines get_min_value_start
when
  grd2:  $get\_min\_value\_add = 0$ 
  grd3:  $prog\_basal = call\_get\_min$ 
with
  t:  $t = par\_get\_t$ 
then
  act1:  $par\_t := par\_get\_t + 1$ 
  act2:  $get\_min\_value\_add := 1$ 

```

```

    act3: get_min_start_t := par_get_t
  end
Event find_min_value ⟨ordinary⟩ ≐
refines find_min_value
  when
    grd1: par_t < c
    grd2: get_min_value_add = 1 ∨ get_min_value_add = 2
    grd3: rate_setting2(par_t) = -1
  then
    act1: par_t := par_t + 1
    act2: get_min_value_add := 2
  end
Event find_min_value_2 ⟨ordinary⟩ ≐
refines find_min_value_2
  when
    grd1: par_t < c
    grd2: get_min_value_add = 1 ∨ get_min_value_add = 2
    grd3: rate_setting2(par_t) ≠ -1
  then
    act1: temp_min := par_t
    act2: get_min_value_add := 3
  end
Event get_max_value ⟨ordinary⟩ ≐
extends get_max_value
  when
    grd2: get_max_value_add = 2
  then
    act1: max_value := rate_setting2(par_t_max)
    act2: get_max_value_add := 0
    act3: prog_basal := return_get_max
  end
Event get_max_value_start ⟨ordinary⟩ ≐
refines get_max_value_start
  when
    grd2: get_max_value_add = 0
    grd3: prog_basal = call_get_max
  with
    t: t = par_get_t
  then
    act1: get_max_start_t := par_get_t
    act2: get_max_value_add := 1
    act3: par_t_max := par_get_t
  end
Event get_max_value_1 ⟨ordinary⟩ ≐
extends get_max_value_1
  when
    grd1: get_max_value_add = 1
    grd3: par_t_max ≥ 0
    grd2: rate_setting2(par_t_max) = -1
  then
    act1: par_t_max := par_t_max - 1
  end
Event get_max_value_2 ⟨ordinary⟩ ≐
extends get_max_value_2
  when
    grd1: get_max_value_add = 1
    grd2: ⟨theorem⟩ par_t_max ≥ 0

```

```
    grd3: rate_setting2(par_t_max) ≠ - 1
  then
    act1: get_max_value_add := 2
  end
END
```

MACHINE Basal6_continuous**REFINES** Basal6**SEES** c_basal2**VARIABLES**

basal_rate_in
 basal_mode
 btime
 rate_setting2
 min_value
 get_min_value_add
 par_t
 temp_min
 get_min_start_t
 max_value
 get_max_start_t
 get_max_value_add
 par_t_max
 prog_basal
 par_get_t
 add_resume
 add_update
 add_start
 fbegin
 fend
 rate_basal_c

INVARIANTS

inv3: $rate_basal_c \in \mathbb{N} \rightarrow 0 .. basal_max$
inv4: $fbegin \in dom(rate_basal_c)$
inv2: $fend \in 0 .. c$
inv5: $rate_basal_c(fbegin) = basal_rate_in$
inv6: $basal_mode = delivering \Rightarrow fend > fbegin$

EVENTS**Initialisation** ⟨extended⟩**begin**

act2: $basal_rate_in := 0$
act3: $basal_mode := stop$
act4: $btime := c$
act5: $rate_setting2 := (1 .. c - 1 \times \{-1\}) \cup \{0 \mapsto 0\}$
act6: $min_value := 0$
act7: $max_value := 0$
act11: $get_min_value_add := 0$
act8: $par_t := 0$
act9: $temp_min := 0$
act10: $get_min_start_t := 0$
act12: $get_max_start_t := 0$
act13: $get_max_value_add := 0$
act14: $par_t_max := 0$
act15: $prog_basal := null$
act16: $par_get_t := 0$
act17: $add_resume := 0$
act18: $add_update := 0$
act19: $add_start := 0$
act20: $fbegin := 0$
act21: $fend := 0$

```

    act22: rate_basal_c := {0 ↦ 0}
  end
Event basal_suspend ⟨ordinary⟩ ≐
extends basal_suspend
  any
    t
  where
    grd1: basal_rate_in ≠ 0
    grd2: basal_mode = delivering
    grd3: prog_basal = null
    grd4: t ∈ fbegin .. fend
  then
    act1: basal_rate_in := 0
    act2: basal_mode := suspended
    act3: rate_basal_c := λx.x ≥ t|0
    act4: fbegin := t
  end
Event change_setting ⟨ordinary⟩ ≐
extends change_setting
  any
    t
    r
  where
    grd5: prog_basal = null
    grd6: t ∈ 0 .. c - 1
    grd7: rate_setting2(t) ≠ -1
    grd2: r ∈ 0 .. basal_max
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ r}
  end
Event delete_setting ⟨ordinary⟩ ≐
extends delete_setting
  any
    t
  where
    grd5: prog_basal = null
    grd2: basal_mode ≠ suspended
    grd6: t ∈ 1 .. c - 1
    grd7: rate_setting2(t) ≠ -1
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ -1}
  end
Event add_setting ⟨ordinary⟩ ≐
extends add_setting
  any
    t
    r
  where
    grd9: prog_basal = null
    grd3: r ∈ 0 .. basal_max
    grd4: basal_mode ≠ suspended
    grd5: t ∈ 0 .. c - 1
    grd6: rate_setting2(t) = -1
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ r}
  end
Event basal_resume_return ⟨ordinary⟩ ≐
extends basal_resume_return

```



```

when
  grd8: prog_basal = return_get_max
  grd9: add_resume = 2
then
  act1: basal_rate_in := max_value
  act2: basal_mode := delivering
  act3: btime := min_value - par_get_t
  act4: prog_basal := null
  act5: add_resume := 0
  act6: rate_basal_c := λx.x ≥ par_get_t ∧ x < min_value|max_value
  act7: fbegin := par_get_t
  act8: fend := min_value
end
Event basal_resume_call ⟨ordinary⟩ ≐
extends basal_resume_call
any
  t
where
  grd4: t ∈ 0 .. c - 1
  grd5: prog_basal = null
  grd6: add_resume = 0
  grd1: basal_rate_in = 0
  grd3: basal_mode = suspended
then
  act1: par_get_t := t
  act2: prog_basal := call_get_min
  act3: add_resume := 1
end
Event basal_resume_call_2 ⟨ordinary⟩ ≐
extends basal_resume_call_2
when
  grd1: prog_basal = return_get_min
  grd2: add_resume = 1
then
  act1: prog_basal := call_get_max
  act2: add_resume := 2
end
Event rate_update_return ⟨ordinary⟩ ≐
extends rate_update_return
when
  grd12: add_update = 1
  grd4: prog_basal = return_get_min
then
  act1: basal_rate_in := rate_setting2(par_get_t)
  act2: btime := min_value - par_get_t
  act3: add_update := 0
  act4: prog_basal := null
  act7: fbegin := par_get_t
  act5: fend := min_value
  act6: rate_basal_c := λx.x ≥ par_get_t ∧ x < min_value|rate_setting2(par_get_t)
end
Event rate_update_call ⟨ordinary⟩ ≐
extends rate_update_call
any
  t
where
  grd6: t ∈ 0 .. c - 1
  grd2: prog_basal = null

```

```

    grd3: add_update = 0
    grd5: basal_mode = delivering
    grd7: rate_setting2(t) ≠ -1
  then
    act1: par_get.t := t
    act2: prog_basal := call_get_min
    act3: add_update := 1
  end
Event start_return ⟨ordinary⟩ ≐
extends start_return
  when
    grd8: add_start = 2
    grd9: prog_basal = return_get_max
  then
    act1: basal_mode := delivering
    act2: basal_rate_in := max_value
    act3: btime := min_value - par_get.t
    act4: add_start := 0
    act5: prog_basal := null
    act8: fbegin := par_get.t
    act6: fend := min_value
    act7: rate_basal.c := λx.x ≥ par_get.t ∧ x < min_value|max_value
  end
Event start_call ⟨ordinary⟩ ≐
extends start_call
  any
    t
  where
    grd1: t ∈ 0..c - 1
    grd2: prog_basal = null
    grd3: add_start = 0
    grd4: basal_mode = stop
  then
    act1: par_get.t := t
    act2: prog_basal := call_get_min
    act3: add_start := 1
  end
Event start_call_2 ⟨ordinary⟩ ≐
extends start_call_2
  when
    grd1: prog_basal = return_get_min
    grd2: add_start = 1
  then
    act1: prog_basal := call_get_max
    act2: add_start := 2
  end
Event stop ⟨ordinary⟩ ≐
extends stop
  any
    t
  where
    grd1: basal_mode = delivering
    grd2: prog_basal = null
    grd3: t ∈ fbegin .. fend
  then
    act1: basal_mode := stop
    act2: basal_rate_in := 0
    act3: fbegin := t

```

```

    act4: rate_basal_c := λx.x ≥ t|0
  end
Event get_min_value_1 ⟨ordinary⟩ ≐
extends get_min_value_1
  when
    grd4: get_min_value_add = 2
    grd5: par.t = c
  then
    act1: min_value := c
    act2: get_min_value_add := 0
    act3: prog_basal := return_get_min
  end
Event get_min_value_2 ⟨ordinary⟩ ≐
extends get_min_value_2
  when
    grd5: get_min_value_add = 3
  then
    act1: min_value := temp_min
    act2: get_min_value_add := 0
    act3: prog_basal := return_get_min
  end
Event get_min_value_start ⟨ordinary⟩ ≐
extends get_min_value_start
  when
    grd2: get_min_value_add = 0
    grd3: prog_basal = call_get_min
  then
    act1: par.t := par_get.t + 1
    act2: get_min_value_add := 1
    act3: get_min_start.t := par_get.t
  end
Event find_min_value ⟨ordinary⟩ ≐
extends find_min_value
  when
    grd1: par.t < c
    grd2: get_min_value_add = 1 ∨ get_min_value_add = 2
    grd3: rate_setting2(par.t) = -1
  then
    act1: par.t := par.t + 1
    act2: get_min_value_add := 2
  end
Event find_min_value_2 ⟨ordinary⟩ ≐
extends find_min_value_2
  when
    grd1: par.t < c
    grd2: get_min_value_add = 1 ∨ get_min_value_add = 2
    grd3: rate_setting2(par.t) ≠ -1
  then
    act1: temp_min := par.t
    act2: get_min_value_add := 3
  end
Event get_max_value ⟨ordinary⟩ ≐
extends get_max_value
  when
    grd2: get_max_value_add = 2
  then
    act1: max_value := rate_setting2(par.t_max)

```

```

    act2: get_max_value_add := 0
    act3: prog_basal := return_get_max
  end
Event get_max_value_start (ordinary)  $\hat{=}$ 
extends get_max_value_start
  when
    grd2: get_max_value_add = 0
    grd3: prog_basal = call_get_max
  then
    act1: get_max_start_t := par_get_t
    act2: get_max_value_add := 1
    act3: par_t_max := par_get_t
  end
Event get_max_value_1 (ordinary)  $\hat{=}$ 
extends get_max_value_1
  when
    grd1: get_max_value_add = 1
    grd3: par_t_max  $\geq$  0
    grd2: rate_setting2(par_t_max) = -1
  then
    act1: par_t_max := par_t_max - 1
  end
Event get_max_value_2 (ordinary)  $\hat{=}$ 
extends get_max_value_2
  when
    grd1: get_max_value_add = 1
    grd2: (theorem) par_t_max  $\geq$  0
    grd3: rate_setting2(par_t_max)  $\neq$  -1
  then
    act1: get_max_value_add := 2
  end
END

```

MACHINE Basal6_continuous_2

add a timer

REFINES Basal6_continuous**SEES** c_basal2**VARIABLES**

basal_rate_in
 basal_mode
 btime
 rate_setting2
 min_value
 get_min_value_add
 par_t
 temp_min
 get_min_start_t
 max_value
 get_max_start_t
 get_max_value_add
 par_t_max
 prog_basal
 par_get_t
 add_resume
 add_update
 add_start
 fbegin
 fend
 rate_basal_c
 time

INVARIANTS

inv1: $time \in 0..c-1$

EVENTS**Initialisation** ⟨extended⟩**begin**

act2: $basal_rate_in := 0$
act3: $basal_mode := stop$
act4: $btime := c$
act5: $rate_setting2 := (1..c-1 \times \{-1\}) \cup \{0 \mapsto 0\}$
act6: $min_value := 0$
act7: $max_value := 0$
act11: $get_min_value_add := 0$
act8: $par_t := 0$
act9: $temp_min := 0$
act10: $get_min_start_t := 0$
act12: $get_max_start_t := 0$
act13: $get_max_value_add := 0$
act14: $par_t_max := 0$
act15: $prog_basal := null$
act16: $par_get_t := 0$
act17: $add_resume := 0$
act18: $add_update := 0$
act19: $add_start := 0$
act20: $fbegin := 0$
act21: $fend := 0$
act22: $rate_basal_c := \{0 \mapsto 0\}$
act23: $time := 0$

end

```

Event change_setting ⟨ordinary⟩ ≐
extends change_setting
  any
    t
    r
  where
    grd5: prog_basal = null
    grd6: t ∈ 0 .. c - 1
    grd7: rate_setting2(t) ≠ -1
    grd2: r ∈ 0 .. basal_max
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ r}
  end
Event delete_setting ⟨ordinary⟩ ≐
extends delete_setting
  any
    t
  where
    grd5: prog_basal = null
    grd2: basal_mode ≠ suspended
    grd6: t ∈ 1 .. c - 1
    grd7: rate_setting2(t) ≠ -1
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ -1}
  end
Event add_setting ⟨ordinary⟩ ≐
extends add_setting
  any
    t
    r
  where
    grd9: prog_basal = null
    grd3: r ∈ 0 .. basal_max
    grd4: basal_mode ≠ suspended
    grd5: t ∈ 0 .. c - 1
    grd6: rate_setting2(t) = -1
  then
    act2: rate_setting2 := rate_setting2 ◁ {t ↦ r}
  end
Event basal_suspend ⟨ordinary⟩ ≐
refines basal_suspend
  when
    grd1: basal_rate_in ≠ 0
    grd2: basal_mode = delivering
    grd3: prog_basal = null
    grd4: time ∈ fbegin .. fend
  with
    t: t = time
  then
    act1: basal_rate_in := 0
    act2: basal_mode := suspended
    act3: rate_basal_c := λx.x ≥ time|0
    act4: fbegin := time
  end
Event basal_resume_return ⟨ordinary⟩ ≐
extends basal_resume_return
  when
    grd8: prog_basal = return_get_max

```

```

    grd9: add_resume = 2
  then
    act1: basal_rate_in := max_value
    act2: basal_mode := delivering
    act3: btime := min_value - par_get_t
    act4: prog_basal := null
    act5: add_resume := 0
    act6: rate_basal_c := λx·x ≥ par_get_t ∧ x < min_value|max_value
    act7: fbegin := par_get_t
    act8: fend := min_value
  end
Event basal_resume_call ⟨ordinary⟩ ≐
refines basal_resume_call
  when
    grd5: prog_basal = null
    grd6: add_resume = 0
    grd1: basal_rate_in = 0
    grd3: basal_mode = suspended
  with
    t: t = time
  then
    act1: par_get_t := time
    act2: prog_basal := call_get_min
    act3: add_resume := 1
  end
Event basal_resume_call_2 ⟨ordinary⟩ ≐
extends basal_resume_call_2
  when
    grd1: prog_basal = return_get_min
    grd2: add_resume = 1
  then
    act1: prog_basal := call_get_max
    act2: add_resume := 2
  end
Event rate_update_return ⟨ordinary⟩ ≐
extends rate_update_return
  when
    grd12: add_update = 1
    grd4: prog_basal = return_get_min
  then
    act1: basal_rate_in := rate_setting2(par_get_t)
    act2: btime := min_value - par_get_t
    act3: add_update := 0
    act4: prog_basal := null
    act7: fbegin := par_get_t
    act5: fend := min_value
    act6: rate_basal_c := λx·x ≥ par_get_t ∧ x < min_value|rate_setting2(par_get_t)
  end
Event rate_update_call ⟨ordinary⟩ ≐
refines rate_update_call
  when
    grd2: prog_basal = null
    grd3: add_update = 0
    grd4: prog_basal = return_get_min
    grd5: basal_mode = delivering
    grd7: rate_setting2(time) ≠ -1
  with
    t: t = time

```

```

    then
      act1: par_get_t := time
      act2: prog_basal := call_get_min
      act3: add_update := 1
    end
  Event start_return ⟨ordinary⟩ ≐
  extends start_return
  when
    grd8: add_start = 2
    grd9: prog_basal = return_get_max
  then
    act1: basal_mode := delivering
    act2: basal_rate.in := max_value
    act3: btime := min_value - par_get_t
    act4: add_start := 0
    act5: prog_basal := null
    act8: fbegin := par_get_t
    act6:  fend := min_value
    act7: rate_basal.c := λx.x ≥ par_get_t ∧ x < min_value|max_value
  end
  Event start_call ⟨ordinary⟩ ≐
  refines start_call
  when
    grd2: prog_basal = null
    grd3: add_start = 0
    grd4: basal_mode = stop
  with
    t: t = time
  then
    act1: par_get_t := time
    act2: prog_basal := call_get_min
    act3: add_start := 1
  end
  Event start_call_2 ⟨ordinary⟩ ≐
  extends start_call_2
  when
    grd1: prog_basal = return_get_min
    grd2: add_start = 1
  then
    act1: prog_basal := call_get_max
    act2: add_start := 2
  end
  Event stop ⟨ordinary⟩ ≐
  refines stop
  when
    grd1: basal_mode = delivering
    grd2: prog_basal = null
    grd3: time ∈ fbegin .. fend
  with
    t: t = time
  then
    act1: basal_mode := stop
    act2: basal_rate.in := 0
    act3: fbegin := time
    act4: rate_basal.c := λx.x ≥ time|0
  end
  Event get_min_value_1 ⟨ordinary⟩ ≐
  extends get_min_value_1

```



```

when
  grd4: get_min_value_add = 2
  grd5: par_t = c
then
  act1: min_value := c
  act2: get_min_value_add := 0
  act3: prog_basal := return_get_min
end
Event get_min_value_2 (ordinary)  $\hat{=}$ 
extends get_min_value_2
  when
    grd5: get_min_value_add = 3
  then
    act1: min_value := temp_min
    act2: get_min_value_add := 0
    act3: prog_basal := return_get_min
  end
Event get_min_value_start (ordinary)  $\hat{=}$ 
extends get_min_value_start
  when
    grd2: get_min_value_add = 0
    grd3: prog_basal = call_get_min
  then
    act1: par_t := par_get.t + 1
    act2: get_min_value_add := 1
    act3: get_min_start.t := par_get.t
  end
Event find_min_value (ordinary)  $\hat{=}$ 
extends find_min_value
  when
    grd1: par_t < c
    grd2: get_min_value_add = 1  $\vee$  get_min_value_add = 2
    grd3: rate_setting2(par_t) = -1
  then
    act1: par_t := par_t + 1
    act2: get_min_value_add := 2
  end
Event find_min_value_2 (ordinary)  $\hat{=}$ 
extends find_min_value_2
  when
    grd1: par_t < c
    grd2: get_min_value_add = 1  $\vee$  get_min_value_add = 2
    grd3: rate_setting2(par_t)  $\neq$  -1
  then
    act1: temp_min := par_t
    act2: get_min_value_add := 3
  end
Event get_max_value (ordinary)  $\hat{=}$ 
extends get_max_value
  when
    grd2: get_max_value_add = 2
  then
    act1: max_value := rate_setting2(par_t_max)
    act2: get_max_value_add := 0
    act3: prog_basal := return_get_max
  end
Event get_max_value_start (ordinary)  $\hat{=}$ 

```

```

extends get_max_value_start
  when
    grd2: get_max_value_add = 0
    grd3: prog_basal = call_get_max
  then
    act1: get_max_start_t := par_get_t
    act2: get_max_value_add := 1
    act3: par_t_max := par_get_t
  end
Event get_max_value_1 (ordinary)  $\hat{=}$ 
extends get_max_value_1
  when
    grd1: get_max_value_add = 1
    grd3: par_t_max  $\geq$  0
    grd2: rate_setting2(par_t_max) = -1
  then
    act1: par_t_max := par_t_max - 1
  end
Event get_max_value_2 (ordinary)  $\hat{=}$ 
extends get_max_value_2
  when
    grd1: get_max_value_add = 1
    grd2: (theorem) par_t_max  $\geq$  0
    grd3: rate_setting2(par_t_max)  $\neq$  -1
  then
    act1: get_max_value_add := 2
  end
Event timer (ordinary)  $\hat{=}$ 
  when
    grd1: time + 1  $\leq$  c - 1
    grd2:
       $\neg$ (
        (add_update = 1)  $\vee$ 
        ((prog_basal = null)  $\wedge$  (add_update = 0)  $\wedge$  (prog_basal = return_get_min)  $\wedge$  (basal_mode = delivering)  $\wedge$  (rate_setting2(time)  $\neq$  -1))
      )
  then
    act1: time := time + 1
  end
Event timer_reset (ordinary)  $\hat{=}$ 
  when
    grd1: time + 1 = c
    grd2:
       $\neg$ (
        (add_update = 1)  $\vee$ 
        ((prog_basal = null)  $\wedge$  (add_update = 0)  $\wedge$  (prog_basal = return_get_min)  $\wedge$  (basal_mode = delivering)  $\wedge$  (rate_setting2(time)  $\neq$  -1))
      )
  then
    act1: time := 0
  end
END

```

MACHINE NormalBolus**SEES** c_normalbolus**VARIABLES**

insulin_needed
 normal_add
 normal_delivering_time
 normal_delivering_rate
 normal_bolus_suspend

INVARIANTS

inv1: $insulin_needed \in \mathbb{N}$
inv5: $normal_add \in 0..3$
inv2: $normal_delivering_time \in \mathbb{N}$
inv3: $normal_delivering_rate \in \mathbb{N}$
inv4: $normal_delivering_rate = 0 \vee normal_delivering_rate = normal_bolus_rate$
inv6: $normal_add = 0 \Rightarrow normal_delivering_rate = 0$
inv7: $normal_add = 1 \Rightarrow insulin_needed \neq 0 \wedge normal_delivering_rate = 0$
inv9: $normal_add = 2 \Rightarrow normal_delivering_rate = 0$
inv8: $normal_add = 3 \Rightarrow normal_delivering_rate = normal_bolus_rate$
inv10: $normal_bolus_suspend \in \text{BOOL}$
inv11: $normal_add = 1 \Rightarrow normal_bolus_suspend = \text{FALSE}$
inv12:
 $normal_add = 2 \Rightarrow normal_bolus_suspend = \text{FALSE}$
inv19: $normal_add = 1 \Rightarrow normal_bolus_suspend = \text{FALSE} \wedge normal_delivering_rate = 0 \wedge normal_delivering_time = 0$
inv20: $normal_add = 2 \Rightarrow normal_bolus_suspend = \text{FALSE} \wedge normal_delivering_rate = 0$
inv21: $normal_add = 3 \Rightarrow normal_bolus_suspend = \text{FALSE} \wedge normal_delivering_rate > 0$
inv22: $normal_add = 0 \Rightarrow normal_delivering_rate = 0 \wedge normal_delivering_time = 0$
inv23: (theorem) $normal_bolus_suspend = \text{TRUE} \Rightarrow normal_add = 0$

EVENTS**Initialisation****begin**

act1: $insulin_needed := 0$
act2: $normal_delivering_time := 0$
act3: $normal_delivering_rate := 0$
act4: $normal_add := 0$
act5: $normal_bolus_suspend := \text{FALSE}$

end**Event** normal_bolus_start_calculate_insulin_needed (ordinary) $\hat{=}$ **any**

insulin

where

grd1: $insulin > 0$
grd3: $normal_add = 0$
grd4: $normal_bolus_suspend = \text{FALSE}$

then

act1: $insulin_needed := insulin$
act2: $normal_add := 1$

end**Event** normal_bolus_start_calculate_lasting_time (ordinary) $\hat{=}$ **when****grd1:** $normal_add = 1$ **then**

act1: $normal_delivering_time := insulin_needed / normal_bolus_rate$
act2: $insulin_needed := 0$
act3: $normal_add := 2$

```
end
Event normal_bolus_delivery ⟨ordinary⟩ ≐
  when
    grd2: normal_add = 2
  then
    act1: normal_delivering_rate := normal_bolus_rate
    act2: normal_add := 3
  end
Event normal_bolus_suspend ⟨ordinary⟩ ≐
  when
    grd4: normal_add = 3
    grd5: normal_bolus_suspend = FALSE
  then
    act1: normal_delivering_rate := 0
    act2: normal_delivering_time := 0
    act3: normal_add := 0
    act4: normal_bolus_suspend := TRUE
  end
Event normal_bolus_finish ⟨ordinary⟩ ≐
  when
    grd4: normal_bolus_suspend = FALSE
    grd3: normal_add = 3
  then
    act1: normal_delivering_rate := 0
    act2: normal_delivering_time := 0
    act3: normal_add := 0
  end
Event normal_bolus_resume ⟨ordinary⟩ ≐
  when
    grd1: normal_bolus_suspend = TRUE
    grd2: normal_add = 0
  then
    act1: normal_bolus_suspend := FALSE
  end
END
```

MACHINE NormalBolus_continuous

REFINES NormalBolus

SEES c_normalbolus_anim

VARIABLES

insulin_needed
 normal_add
 normal_delivering_time
 normal_delivering_rate
 normal_delivering_rate_c
 nb_now
 nb_new_now
 normal_bolus_suspend

INVARIANTS

inv1: $normal_delivering_rate_c \in \mathbb{N} \mapsto 0 .. normal_bolus_rate$
inv3: $nb_new_now \in \mathbb{N}$
inv5: $nb_now \in dom(normal_delivering_rate_c)$
inv4: $normal_delivering_rate_c(nb_now) = normal_delivering_rate$

EVENTS

Initialisation (extended)

begin

act1: $insulin_needed := 0$
act2: $normal_delivering_time := 0$
act3: $normal_delivering_rate := 0$
act4: $normal_add := 0$
act5: $normal_bolus_suspend := FALSE$
act8: $normal_delivering_rate_c := \{0 \mapsto 0\}$
act6: $nb_now := 0$
act7: $nb_new_now := 0$

end

Event normal_bolus_start_calculate_insulin_needed (ordinary) $\hat{=}$

extends normal_bolus_start_calculate_insulin_needed

any

insulin

where

grd1: $insulin > 0$
grd3: $normal_add = 0$
grd4: $normal_bolus_suspend = FALSE$

then

act1: $insulin_needed := insulin$
act2: $normal_add := 1$

end

Event normal_bolus_start_calculate_lasting_time (ordinary) $\hat{=}$

extends normal_bolus_start_calculate_lasting_time

when

grd1: $normal_add = 1$

then

act1: $normal_delivering_time := insulin_needed / normal_bolus_rate$
act2: $insulin_needed := 0$
act3: $normal_add := 2$

end

Event normal_bolus_delivery (ordinary) $\hat{=}$

extends normal_bolus_delivery

when

grd2: $normal_add = 2$

then

```

    act1: normal_delivering_rate := normal_bolus_rate
    act2: normal_add := 3
    act3: normal_delivering_rate.c :=  $\lambda t \cdot t \in \text{nb\_now}.. \text{nb\_now} + \text{normal\_delivering\_time} | \text{normal\_bolus\_rate}$ 

    act5: nb_new_now := nb_now + normal_delivering_time
  end
Event normal_bolus_suspend  $\langle \text{ordinary} \rangle \hat{=}$ 
extends normal_bolus_suspend
  any
    ta
  where
    grd4: normal_add = 3
    grd5: normal_bolus_suspend = FALSE
    grd7: ta  $\in$  nb_now .. nb_new_now
  then
    act1: normal_delivering_rate := 0
    act2: normal_delivering_time := 0
    act3: normal_add := 0
    act4: normal_bolus_suspend := TRUE
    act6: normal_delivering_rate.c :=  $\lambda t \cdot t \geq \text{ta} | 0$ 
    act5: nb_now := ta
  end
Event normal_bolus_finish  $\langle \text{ordinary} \rangle \hat{=}$ 
extends normal_bolus_finish
  any
    ta
  where
    grd4: normal_bolus_suspend = FALSE
    grd3: normal_add = 3
    grd5: ta = nb_new_now
  then
    act1: normal_delivering_rate := 0
    act2: normal_delivering_time := 0
    act3: normal_add := 0
    act4: normal_delivering_rate.c :=  $\lambda t \cdot t \geq \text{ta} | 0$ 
    act5: nb_now := ta
  end
Event normal_bolus_resume  $\langle \text{ordinary} \rangle \hat{=}$ 
extends normal_bolus_resume
  any
    ta
  where
    grd1: normal_bolus_suspend = TRUE
    grd2: normal_add = 0
    grd3: ta  $\geq$  nb_now
  then
    act1: normal_bolus_suspend := FALSE
    act2: nb_now := ta
    act3: normal_delivering_rate.c :=  $\lambda t \cdot t \geq \text{ta} | 0$ 
  end
END

```

MACHINE NormalBolus_continuous_2

REFINES NormalBolus_continuous

SEES c_normalbolus_anim

VARIABLES

insulin_needed
 normal_add
 normal_delivering_time
 normal_delivering_rate
 normal_delivering_rate_c
 nb_now
 nb_new_now
 normal_bolus_suspend
 time
 t_normal

INVARIANTS

inv1: $time \in \mathbb{N}$
inv2: $t_normal \in \mathbb{N}$

EVENTS

Initialisation (extended)

begin

act1: $insulin_needed := 0$
act2: $normal_delivering_time := 0$
act3: $normal_delivering_rate := 0$
act4: $normal_add := 0$
act5: $normal_bolus_suspend := FALSE$
act8: $normal_delivering_rate_c := \{0 \mapsto 0\}$
act6: $nb_now := 0$
act7: $nb_new_now := 0$
act9: $time := 0$
act10: $t_normal := 0$

end

Event normal_bolus_start_calculate_insulin_needed (ordinary) $\hat{=}$

extends normal_bolus_start_calculate_insulin_needed

any

insulin

where

grd1: $insulin > 0$
grd3: $normal_add = 0$
grd4: $normal_bolus_suspend = FALSE$

then

act1: $insulin_needed := insulin$
act2: $normal_add := 1$

end

Event normal_bolus_start_calculate_lasting_time (ordinary) $\hat{=}$

extends normal_bolus_start_calculate_lasting_time

when

grd1: $normal_add = 1$

then

act1: $normal_delivering_time := insulin_needed / normal_bolus_rate$
act2: $insulin_needed := 0$
act3: $normal_add := 2$

end

Event normal_bolus_delivery (ordinary) $\hat{=}$

extends normal_bolus_delivery

when

```

    grd2: normal_add = 2
  then
    act1: normal_delivering_rate := normal_bolus_rate
    act2: normal_add := 3
    act3: normal_delivering_rate.c := λt.t ∈ nb_now..nb_now+normal_delivering_time|normal_bolus_rate

    act5: nb_new_now := nb_now + normal_delivering_time
    act6: t_normal := time + normal_delivering_time
  end
Event normal_bolus_suspend ⟨ordinary⟩ ≐
refines normal_bolus_suspend
  when
    grd4: normal_add = 3
    grd5: normal_bolus_suspend = FALSE
    grd7: time ∈ nb_now .. nb_new_now
  with
    ta: ta = time
  then
    act1: normal_delivering_rate := 0
    act2: normal_delivering_time := 0
    act3: normal_add := 0
    act4: normal_bolus_suspend := TRUE
    act6: normal_delivering_rate.c := λt.t ≥ time|0
    act5: nb_now := time
  end
Event normal_bolus_finish ⟨ordinary⟩ ≐
refines normal_bolus_finish
  when
    grd4: normal_bolus_suspend = FALSE
    grd3: normal_add = 3
    grd5: time = nb_new_now
    grd6: t_normal = time
  with
    ta: ta = time
  then
    act1: normal_delivering_rate := 0
    act2: normal_delivering_time := 0
    act3: normal_add := 0
    act4: normal_delivering_rate.c := λt.t ≥ time|0
    act5: nb_now := time
  end
Event normal_bolus_resume ⟨ordinary⟩ ≐
refines normal_bolus_resume
  when
    grd1: normal_bolus_suspend = TRUE
    grd2: normal_add = 0
    grd3: time ≥ nb_now
  with
    ta: ta = time
  then
    act1: normal_bolus_suspend := FALSE
    act2: nb_now := time
    act3: normal_delivering_rate.c := λt.t ≥ time|0
  end
Event timer ⟨ordinary⟩ ≐
begin
  act1: time := time + 1
end
END

```