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CONTEXT c0

SETS

CLOCKS

CONSTANTS

Infinity

AXIOMS

axm1: $Infinity > 0$

axm2: $Infinity \geq 100$

for animb

END

CONTEXT belt_c0_clks

EXTENDS c0

CONSTANTS

bclks

b1

b2

tb

tp

AXIOMS

axm2: $bclks \subseteq CLOCKS$

axm1: $partition(bclks, \{b1\}, \{b2\})$

axm4: $tb > 0$

axm5: $tp > 0$

axm6: $tb \geq 5$

for aminb

axm7: $tp \geq 2$

for aminb

END

CONTEXT belt_press_c

EXTENDS belt_c0_clks,press_c1_clks

AXIOMS

axm5: $pclks \cap bclks = \emptyset$
new added one

END

CONTEXT press_c0

CONSTANTS

bottom

middle

top

AXIOMS

axm3: $bottom \in \mathbb{R}$

axm4: $middle \in \mathbb{R}$

axm5: $top \in \mathbb{R}$

axm6: $top > middle$

axm7: $middle > bottom$

axm8: *(theorem)* $top > bottom$

END

MACHINE press0

SEES press_c0

VARIABLES

position
work1
work3
work2

INVARIANTS

inv1: position \in {bottom, middle, top}
inv4: work1 = TRUE \Rightarrow *position = middle*
inv5: work2 = TRUE \Rightarrow *position = top*
inv6: work3 = TRUE \Rightarrow *position = bottom*

EVENTS

Initialisation

begin

act2: position := middle
act5: work1 := FALSE
act6: work3 := FALSE
act7: work2 := FALSE

end

Event Loading_start \langle ordinary $\rangle \hat{=}$

when

grd1: position = middle
grd3: work1 = FALSE

then

act2: work1 := TRUE

end

Event Loading \langle ordinary $\rangle \hat{=}$

when

grd2: work1 = TRUE

then

act1: position := top
act2: work1 := FALSE

end

Event Pressing_start \langle ordinary $\rangle \hat{=}$

when

grd1: position = top
grd2: work2 = FALSE

then

act1: work2 := TRUE

end

Event Pressing \langle ordinary $\rangle \hat{=}$

when

grd1: work2 = TRUE

then

act2: position := bottom
act3: work2 := FALSE

end

Event Unloading_start \langle ordinary $\rangle \hat{=}$

when

grd1: position = bottom
grd3: work3 = FALSE

then

act2: work3 := TRUE

end

Event Unloading \langle ordinary $\rangle \hat{=}$

```
when
  grd2: work3 = TRUE
then
  act2: position := middle
  act3: work3 := FALSE
end
END
```

MACHINE press1

Using time and Click

REFINES press0**SEES** press_c1_clks**VARIABLES**

position

work1

work2

work3

lbTimer2

now

ubTimer2

INVARIANTS**inv12:** $lbTimer2 \in \{p1, p2, p3\} \rightarrow \mathbb{R}$ **inv13:** $now \in \mathbb{R}$ **inv9:** $work1 = FALSE \Rightarrow lbTimer2(p1) = 0$ **inv10:** $work2 = FALSE \Rightarrow lbTimer2(p2) = 0$ **inv11:** $work3 = FALSE \Rightarrow lbTimer2(p3) = 0$ **inv14:** $ubTimer2 \in \{p1, p2, p3\} \rightarrow \mathbb{R}$ **EVENTS****Initialisation** ⟨extended⟩**begin****act2:** $position := middle$ **act5:** $work1 := FALSE$ **act6:** $work3 := FALSE$ **act7:** $work2 := FALSE$ **act15:** $lbTimer2 := \{p1 \mapsto 0, p2 \mapsto 0, p3 \mapsto 0\}$ **act16:** $now := 0$ **act17:** $ubTimer2 := \{p1 \mapsto ubTa, p2 \mapsto Infinity, p3 \mapsto Infinity\}$ **end****Event** Loading_start ⟨ordinary⟩ $\hat{=}$ **extends** Loading_start**when****grd1:** $position = middle$ **grd3:** $work1 = FALSE$ **then****act2:** $work1 := TRUE$ **act7:** $lbTimer2(p1) := lbTa$ **act8:** $ubTimer2(p1) := ubTa$ **end****Event** Loading ⟨ordinary⟩ $\hat{=}$ **extends** Loading**when****grd2:** $work1 = TRUE$ **grd5:** $lbTimer2(p1) = 0$ **then****act1:** $position := top$ **act2:** $work1 := FALSE$ **act3:** $ubTimer2(p1) := Infinity$ **end****Event** Pressing_start ⟨ordinary⟩ $\hat{=}$ **extends** Pressing_start**when****grd1:** $position = top$ **grd2:** $work2 = FALSE$


```

    then
      act1: work2 := TRUE
      act4: lbTimer2(p2) := lbTb
      act5: ubTimer2(p2) := ubTb
    end
  Event Pressing ⟨ordinary⟩ ≐
  extends Pressing
  when
    grd1: work2 = TRUE
    grd4: lbTimer2(p2) = 0
  then
    act2: position := bottom
    act3: work2 := FALSE
    act4: ubTimer2(p2) := Infinity
  end
  Event Unloading_start ⟨ordinary⟩ ≐
  extends Unloading_start
  when
    grd1: position = bottom
    grd3: work3 = FALSE
  then
    act2: work3 := TRUE
    act6: lbTimer2(p3) := lbTc
    act7: ubTimer2(p3) := ubTc
  end
  Event Unloading ⟨ordinary⟩ ≐
  extends Unloading
  when
    grd2: work3 = TRUE
    grd5: lbTimer2(p3) = 0
  then
    act2: position := middle
    act3: work3 := FALSE
    act4: ubTimer2(p3) := Infinity
  end
  Event Click ⟨ordinary⟩ ≐
  any
    w
  where
    grd1: w > 0
    grd2: w ≤ min(ran(ubTimer2))
  then
    act1: now := now + w
    act2: lbTimer2 := {c ↦ v | c ∈ dom(lbTimer2) ∧ v = max({0, lbTimer2(c) - w})}
    act3: ubTimer2 := ubTimer2 ⋄ {c ↦ v | c ∈ dom(ubTimer2) ⋄ {Infinity}} ∧ v = ubTimer2(c) - w
  end
END

```

MACHINE belt0**SEES** belt_c0_clks**VARIABLES**

sensor1
 lbTimer0
 now
 ubTimer0

INVARIANTS**inv2:** $sensor1 \in \text{BOOL}$ **inv4:** $lbTimer0 \in \{b1\} \rightarrow \mathbb{R}$ **inv5:** $now \in \mathbb{R}$ **inv6:** $ubTimer0 \in \{b1\} \rightarrow \mathbb{R}$ **DLF:**

(
 (($sensor1 = \text{FALSE}$) \wedge ($lbTimer0(b1) = 0$)) \vee
 ($sensor1 = \text{TRUE}$) \vee
 ($\exists w. ((w > 0) \wedge (w \leq \min(\text{ran}(ubTimer0))))$)
)

inv7: $\langle \text{theorem} \rangle \min(\text{ran}(ubTimer0)) = 0 \Rightarrow ubTimer0(b1) = 0$ **inv8:** $ubTimer0(b1) = 0 \Rightarrow sensor1 = \text{TRUE}$ **inv9:** $sensor1 = \text{FALSE} \Rightarrow ubTimer0(b1) = \text{Infinity}$ **EVENTS****Initialisation****begin**

act1: $sensor1 := \text{TRUE}$
act3: $lbTimer0 := \{b1 \mapsto 0\}$
act4: $now := 0$
act5: $ubTimer0 := \{b1 \mapsto \text{Infinity}\}$

end**Event** Belt_1 $\langle \text{ordinary} \rangle \hat{=}$ **when**

grd1: $sensor1 = \text{FALSE}$
grd2: $lbTimer0(b1) = 0$

then

act1: $sensor1 := \text{TRUE}$
act2: $lbTimer0(b1) := tb$
act3: $ubTimer0(b1) := tp$

end**Event** loading_start $\langle \text{ordinary} \rangle \hat{=}$ **when****grd1:** $sensor1 = \text{TRUE}$ **then**

act1: $sensor1 := \text{FALSE}$
act2: $ubTimer0(b1) := \text{Infinity}$

end**Event** Click $\langle \text{ordinary} \rangle \hat{=}$ **any****w****where**

grd5: $w > 0$
grd6: $w \leq \min(\text{ran}(ubTimer0))$

then

act1: $lbTimer0 := \{c \mapsto v \mid c \in \text{dom}(lbTimer0) \wedge v = \max(\{0, lbTimer0(c) - w\})\}$
act3: $ubTimer0 := ubTimer0 \triangleleft \{c \mapsto v \mid c \in \text{dom}(ubTimer0) \triangleright \{\text{Infinity}\}\} \wedge v = ubTimer0(c) - w$
act2: $now := now + w$

end**END**

MACHINE belt1**REFINES** belt0**SEES** belt_c0_clks**VARIABLES**

sensor1
 sensor2
 lbTimer1
 now
 ubTimer1
 lbTimer0
 ubTimer0

INVARIANTS

inv3: $lbTimer1 \in \{b1, b2\} \rightarrow \mathbb{R}$
inv4: $ubTimer1 \in \{b1, b2\} \rightarrow \mathbb{R}$
inv5: $sensor2 \in \text{BOOL}$
inv1: $lbTimer0 \subseteq lbTimer1$
inv2: $ubTimer0 \subseteq ubTimer1$

EVENTS**Initialisation** ⟨extended⟩**begin**

act1: $sensor1 := \text{TRUE}$
act3: $lbTimer0 := \{b1 \mapsto 0\}$
act4: $now := 0$
act5: $ubTimer0 := \{b1 \mapsto \text{Infinity}\}$
act6: $sensor2 := \text{FALSE}$
act7: $lbTimer1 := \{b1 \mapsto 0, b2 \mapsto 0\}$
act8: $ubTimer1 := \{b1 \mapsto \text{Infinity}, b2 \mapsto \text{Infinity}\}$

end**Event** Belt_1 ⟨ordinary⟩ $\hat{=}$ **extends** Belt_1**when**

grd1: $sensor1 = \text{FALSE}$
grd2: $lbTimer0(b1) = 0$
grd3: $lbTimer1(b1) = 0$

then

act1: $sensor1 := \text{TRUE}$
act2: $lbTimer0(b1) := tb$
act3: $ubTimer0(b1) := tp$
act4: $lbTimer1(b1) := tb$
act5: $ubTimer1(b1) := tp$

end**Event** loading_start ⟨ordinary⟩ $\hat{=}$ **extends** loading_start**when**

grd1: $sensor1 = \text{TRUE}$

then

act1: $sensor1 := \text{FALSE}$
act2: $ubTimer0(b1) := \text{Infinity}$
act3: $ubTimer1(b1) := \text{Infinity}$

end**Event** Belt_2 ⟨ordinary⟩ $\hat{=}$ **when**

grd1: $sensor2 = \text{TRUE}$
grd2: $lbTimer1(b2) = 0$

then

```

    act1: sensor2 := FALSE
    act2: lbTimer1(b2) := tb
    act3: ubTimer1(b2) := tp
  end
Event unloading_start ⟨ordinary⟩ ≐
  when
    grd1: sensor2 = FALSE
  then
    act1: sensor2 := TRUE
    act2: ubTimer1(b2) := Infinity
  end
Event Click ⟨ordinary⟩ ≐
refines Click
  any
    w
  where
    grd5: w > 0
    grd7: w ≤ min(ran(ubTimer1))
    grd6: ⟨theorem⟩ w ≤ min(ran(ubTimer0))
  then
    act1: lbTimer0 := {c ↦ v | c ∈ dom(lbTimer0) ∧ v = max({0, lbTimer0(c) - w})}
    act3: ubTimer0 := ubTimer0 ⇐ {c ↦ v | c ∈ dom(ubTimer0) ⊇ {Infinity}} ∧ v = ubTimer0(c) - w
    act2: now := now + w
    act4: lbTimer1 := {c ↦ v | c ∈ dom(lbTimer1) ∧ v = max({0, lbTimer1(c) - w})}
    act5: ubTimer1 := ubTimer1 ⇐ {c ↦ v | c ∈ dom(ubTimer1) ⊇ {Infinity}} ∧ v = ubTimer1(c) - w
  end
END

```

MACHINE belt2

REFINES belt1

SEES belt_c0_clks

VARIABLES

sensor1
 sensor2
 lbTimer1
 now
 ubTimer1

EVENTS

Initialisation

begin

act1: $sensor1 := TRUE$
act4: $now := 0$
act6: $sensor2 := FALSE$
act7: $lbTimer1 := \{b1 \mapsto 0, b2 \mapsto 0\}$
act8: $ubTimer1 := \{b1 \mapsto Infinity, b2 \mapsto Infinity\}$

end

Event Belt_1 \langle ordinary $\rangle \hat{=}$

refines Belt_1

when

grd1: $sensor1 = FALSE$
grd3: $lbTimer1(b1) = 0$

then

act1: $sensor1 := TRUE$
act4: $lbTimer1(b1) := tb$
act5: $ubTimer1(b1) := tp$

end

Event loading_start \langle ordinary $\rangle \hat{=}$

refines loading_start

when

grd1: $sensor1 = TRUE$

then

act1: $sensor1 := FALSE$
act3: $ubTimer1(b1) := Infinity$

end

Event Belt_2 \langle ordinary $\rangle \hat{=}$

extends Belt_2

when

grd1: $sensor2 = TRUE$
grd2: $lbTimer1(b2) = 0$

then

act1: $sensor2 := FALSE$
act2: $lbTimer1(b2) := tb$
act3: $ubTimer1(b2) := tp$

end

Event unloading_start \langle ordinary $\rangle \hat{=}$

extends unloading_start

when

grd1: $sensor2 = FALSE$

then

act1: $sensor2 := TRUE$
act2: $ubTimer1(b2) := Infinity$

end

Event Click \langle ordinary $\rangle \hat{=}$

refines Click

```
any
  w
where
  grd5:  $w > 0$ 
  grd7:  $w \leq \min(\text{ran}(\text{ubTimer1}))$ 
then
  act2:  $\text{now} := \text{now} + w$ 
  act4:  $\text{lbTimer1} := \{c \mapsto v \mid c \in \text{dom}(\text{lbTimer1}) \wedge v = \max(\{0, \text{lbTimer1}(c) - w\})\}$ 
  act5:  $\text{ubTimer1} := \text{ubTimer1} \triangleleft \{c \mapsto v \mid c \in \text{dom}(\text{ubTimer1}) \triangleright \{\text{Infinity}\} \wedge v = \text{ubTimer1}(c) - w\}$ 
end
END
```

MACHINE belt2_press1**REFINES** belt2**SEES** belt_press_c**VARIABLES**

sensor1
 position
 work1
 work2
 work3
 lbTimer2
 now
 ubTimer2
 sensor2
 lbTimer1
 ubTimer1

INVARIANTS

inv0: $work2 \in \text{BOOL}$
inv1: $now \in \mathbb{Z}$
inv2: $position \in \mathbb{Z}$
inv3: $sensor2 \in \text{BOOL}$
inv4: $ubTimer2 \in \mathbb{P}(\text{CLOCKS} \times \mathbb{Z})$
inv5: $sensor1 \in \text{BOOL}$
inv6: $lbTimer1 \in \mathbb{P}(\text{CLOCKS} \times \mathbb{Z})$
inv7: $work1 \in \text{BOOL}$
inv8: $work3 \in \text{BOOL}$
inv9: $lbTimer2 \in \mathbb{P}(\text{CLOCKS} \times \mathbb{Z})$
inv12: $lbTimer2 \in \text{pcls} \rightarrow \mathbb{R}$
inv14: $ubTimer2 \in \text{pcls} \rightarrow \mathbb{R}$
inv10: $ubTimer1 \in \text{bcls} \rightarrow \mathbb{R}$

EVENTS**Initialisation****begin**

belt2.act1: $sensor1 := \text{TRUE}$
press1.act2: $position := \text{middle}$
press1.act5: $work1 := \text{FALSE}$
press1.act6: $work3 := \text{FALSE}$
press1.act7: $work2 := \text{FALSE}$
press1.act15: $lbTimer2 := \{p1 \mapsto 0, p2 \mapsto 0, p3 \mapsto 0\}$
press1.act16: $now := 0$
press1.act17: $ubTimer2 := \{p1 \mapsto \text{ubTa}, p2 \mapsto \text{Infinity}, p3 \mapsto \text{Infinity}\}$
belt2.act2: $sensor2 := \text{FALSE}$
belt2.act3: $lbTimer1 := \{b1 \mapsto 0, b2 \mapsto 0\}$
belt2.act5: $ubTimer1 := \{b1 \mapsto \text{Infinity}, b2 \mapsto \text{Infinity}\}$

end**Event** belt2.Belt_1 *(ordinary)* $\hat{=}$ **refines** Belt_1**when**

belt2.grd1: $sensor1 = \text{FALSE}$
belt2.grd2: $lbTimer1(b1) = 0$

then

belt2.act1: $sensor1 := \text{TRUE}$
belt2.act2: $lbTimer1(b1) := tb$
act3: $ubTimer1(b1) := tp$

end

```

Event belt2·Belt_2 ⟨ordinary⟩ ≐
refines Belt_2
  when
    belt2.grd1: sensor2 = TRUE
    belt2.grd2: lbTimer1(b2) = 0
  then
    belt2.act1: sensor2 := FALSE
    belt2.act2: lbTimer1(b2) := tb
    belt2.act3: ubTimer1(b2) := tp
  end
Event belt2·loading_start_press1·Loading_start ⟨ordinary⟩ ≐
refines loading_start
  when
    belt2.grd1: sensor1 = TRUE
    press1.grd1: position = middle
    press1.grd3: work1 = FALSE
  then
    press1.act2: work1 := TRUE
    press1.act7: lbTimer2(p1) := lbTa
    belt2.act1: sensor1 := FALSE
    press1.act8: ubTimer2(p1) := ubTa
    belt2.act2: ubTimer1(b1) := Infinity
  end
Event belt2·unloading_start_press1·Unloading_start ⟨ordinary⟩ ≐
refines unloading_start
  when
    press1.grd1: position = bottom
    belt2.grd1: sensor2 = FALSE
    press1.grd3: work3 = FALSE
  then
    press1.act2: work3 := TRUE
    press1.act6: lbTimer2(p3) := lbTc
    belt2.act1: sensor2 := TRUE
    press1.act7: ubTimer2(p3) := ubTc
    belt2.act2: ubTimer1(b2) := Infinity
  end
Event press1·Loading ⟨ordinary⟩ ≐
  when
    press1.grd2: work1 = TRUE
    press1.grd5: lbTimer2(p1) = 0
  then
    press1.act1: position := top
    press1.act2: work1 := FALSE
    press1.act3: ubTimer2(p1) := Infinity
  end
Event press1·Pressing_start ⟨ordinary⟩ ≐
  when
    press1.grd1: position = top
    press1.grd2: work2 = FALSE
  then
    press1.act1: work2 := TRUE
    press1.act4: lbTimer2(p2) := lbTb
    press1.act5: ubTimer2(p2) := ubTb
  end
Event press1·Pressing ⟨ordinary⟩ ≐
  when
    press1.grd1: work2 = TRUE
    press1.grd4: lbTimer2(p2) = 0

```



```

    then
      press1.act2: position := bottom
      press1.act3: work2 := FALSE
      press1.act4: ubTimer2(p2) := Infinity
    end
  Event press1.Unloading ⟨ordinary⟩ ≐
  when
    press1.grd2: work3 = TRUE
    press1.grd5: lbTimer2(p3) = 0
  then
    press1.act2: position := middle
    press1.act3: work3 := FALSE
    press1.act4: ubTimer2(p3) := Infinity
  end
  Event belt2.Click_press1.Click ⟨ordinary⟩ ≐
  refines Click
  any
    w
  where
    belt2.grd5:  $w > 0$ 
    press1.grd2:  $w \leq \min(\text{ran}(\text{ubTimer2}))$ 
    grd6:  $w \leq \min(\text{ran}(\text{ubTimer1}))$ 
  then
    belt2.act2: now := now + w
    belt2.act1:  $\text{lbTimer1} := \text{lbTimer1} \Leftarrow \{c \mapsto v \mid c \in \text{bclks} \wedge v = \max(\{0, \text{lbTimer1}(c) - w\})\}$ 
    press1.act2:  $\text{lbTimer2} := \{c \mapsto v \mid c \in \text{dom}(\text{lbTimer2}) \wedge v = \max(\{0, \text{lbTimer2}(c) - w\})\}$ 
    press1.act3:  $\text{ubTimer2} := \text{ubTimer2} \Leftarrow \{c \mapsto v \mid c \in \text{dom}(\text{ubTimer2}) \wedge v = \text{ubTimer2}(c) - w\}$ 
    belt2.act3:  $\text{ubTimer1} := \text{ubTimer1} \Leftarrow \{c \mapsto v \mid c \in \text{dom}(\text{ubTimer1}) \wedge v = \text{ubTimer1}(c) - w\}$ 
  end
END

```