

$$\frac{}{r([\text{var}_1 = \text{var}_2, \Sigma] | \text{Stack}, \sigma) \rightarrow ([\text{Stack}], \sigma + (\text{var}_1, \text{var}_2))} \text{var-var binding}$$

$$\frac{\text{var}' \text{ is a fresh variable} \quad \sigma' = \sigma + (\text{var}', \text{simplify}(\text{value}, \sigma))}{([\text{var} = \text{value}, \Sigma] | \text{Stack}, \sigma) \rightarrow ([\text{Stack}], \sigma')} \text{var-value binding}$$

where  $\text{simplify}(v, \sigma)$  replaces instances of variables in  $v$  with the values they're bound to in  $\sigma$ .

(This is where unification is done).

$$\frac{\Sigma(\text{var}) \text{ is not a boolean}}{\text{if-error}}$$

$$([\text{if var then } S_1 \text{ else } S_2 \text{ end}, \Sigma] | \text{Stack}, \sigma) \rightarrow \text{error}$$

$$\frac{\Sigma(\text{var}) \text{ is true}}{\text{if-true}}$$

$$([\text{if var then } S_1 \text{ else } S_2 \text{ end}, \Sigma] | \text{Stack}, \sigma) \rightarrow ([S_1, \Sigma] | \text{Stack}, \sigma)$$

$$\frac{\Sigma(\text{var}) \text{ is false}}{\text{if-false}}$$

$$([\text{if var then } S_1 \text{ else } S_2 \text{ end}, \Sigma] | \text{Stack}, \sigma) \rightarrow ([S_2, \Sigma] | \text{Stack}, \sigma)$$

(If  $\Sigma(\text{var})$  is a partial boolean, we cannot continue (yet).)

$\Sigma(f)$  is not a procedure

proc-error

$([(\Sigma f \ x_1 \dots x_n \}, \Sigma) \mid \text{Stack}], \sigma) \rightarrow \text{error}$

$\Sigma(f)$  has form  $(\text{proc } \Sigma \ \$ \ y_1 \dots y_n \} \ S \ \text{end}, \Sigma')$

$([(\Sigma f \ x_1 \dots x_n \}, \Sigma) \mid \text{Stack}], \sigma) \rightarrow ([(\Sigma', \Sigma' [y_1, \dots, y_n := \Sigma(x_1), \dots, \Sigma(x_n)] \mid \text{Stack}], \sigma)$

$m \neq n$   $\Sigma(f)$  has form  $(\text{proc } \Sigma \ \$ \ y_1 \dots y_m \} \ S \ \text{end}, \Sigma')$

$([(\Sigma f \ x_1 \dots x_n \}, \Sigma) \mid \text{Stack}], \sigma) \rightarrow \text{error}$