

## COMP SCI/SFWR ENG 4/6E03 — Assignment 11

1. Consider the Dining Philosophers Problem. Five philosophers are seated around a circular table and are dining with chopsticks. A chopstick is placed on the table between each philosopher. Each philosopher spends an exponentially distributed period of time (with rate  $\lambda$ ) thinking, then tries to acquire the chopsticks to the left and right in order to eat. The time spent eating is exponentially distributed with rate  $\mu$ . After eating, the philosopher relinquishes the chopsticks and starts thinking again (where the whole process of thinking/eating repeats).
  - (a) Model this as an SPN. Note that you will have to make sure your implementation is deadlock-free.
  - (b) Draw the state transition diagram (do not solve for the steady-state probabilities).
  
2. Consider a two processor system with shared memory. Each processor executes locally for some time (exponentially distributed with mean  $1/\lambda$ ) and then requests access to shared memory (request times are exponentially distributed with mean  $1/r$ ). Once a processor has gained access, the duration of the shared memory access is assumed to be exponentially distributed with mean  $1/\mu$ . (Note that only one processor can have access to the shared memory at a given time.)
  - (a) Model this system as an SPN.
  - (b) In steady-state, what is the probability that the shared memory is *not* being accessed? (For concreteness, let  $\lambda = 0.1$ ,  $r = 1$ ,  $\mu = 0.1$ .)