

## CAS 743 — Functional Programming

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We define a type of transition functions that define state transitions triggered by *inputs* and also producing *outputs*:

**type** *Transition state input output* = ( *state*, *input* ) → ( *state*, *output* )

(a) Define a Haskell function

*process* :: *Transition state input output* → *state* → [ *input* ] → [ *output* ]

that calculates the list of outputs produced by a transition function given a starting state and a list of inputs.

Using *process* from (a) and prelude functions, the definition

*runprocess* :: *Transition state String String* → *state* → IO ()

*runprocess tr s* = **do**

*hSetBuffering stdout LineBuffering* -- requires: "import System.IO" at beginning of module  
*interact ( unlines ∘ process tr s ∘ lines )*

allows *runprocess* to turn a transition with *String* inputs and outputs into a runnable program.

Try: *runprocess id 0*

(b) Define a transition function

*countEcho* :: *Transition Integer String String*

that keeps a counter as its state and otherwise just reproduces the input prefixed with line numbers as output.

Try: *runprocess countEcho 0*

(c) Define a transition function

*trAdd* :: *Transition Integer String String*

that uses the prelude functions *read* and *show* to add the *Integer* reading of the input to the accumulating state, and outputs that state as a string.

Try: *runprocess trAdd 0*

(d) For finite *state*, *input*, and *output* types, the *Transition* type defined above is the type of the transition function of a deterministic Mealy automaton.

Let us use the following type for explicit representations of such transition functions:

**type** *Mealy state input output* = [ ( ( *state*, *input* ), ( *state*, *output* ) ) ]

Define a transition function generator

*trMealy* :: ( *Eq state* ) ⇒ *Mealy state String String* → *Transition state String String*

that turns a representation of a Mealy transition function with *String* inputs and outputs into the corresponding *Transition*.

Define a non-trivial Mealy transition function and try: *runprocess ( trMealy myMealy ) state0*

- (e) Let the following type for representing finite-state machines (parameterised with the *state* type) be given:

```
type FSM state = ( state, [ state ], [ (( state, String), state) ])
```

Define a transition function generator

```
trDFSM :: ( Eq state, Show state ) => FSM state -> Transition state String String
```

that, given a representation of a **deterministic** finite-state machine, produces a transition function that takes input symbols for the FSM as inputs, and *shows* the current state as output, together with information whether the current state is final.

Define a non-trivial FSM and try: `runprocess ( trDFSM myFSM ) myStartState`

- (f) Produce *trNFSM* by modifying *trDFSM* to produce appropriate transitions also for **non-deterministic** finite-state machines.

- (g) Define a transition function

```
polish :: Transition [ Integer ] String String
```

that implements a reverse Polish notation calculator by pushing number inputs on the stack, always outputting the top of the stack (if present), and interpreting +, -, \*, / as taking their arguments from the stack and pushing the result back onto the stack.

Try: `runprocess polish [ ]`

- (h) **(optional)** Instead of only showing the top element of the stack in your implementation of *polish*, output the top five elements on the stack (as far as present). Also include in your solution for *polish* some stack manipulation commands, such as

- “dup” pushes the top element of the stack onto the stack another time,
- “exch” swaps the two top element on the stack,
- “rot” pops the top element, say *n*, from the stack, and then rotates the top *n* remaining elements “downwards”.