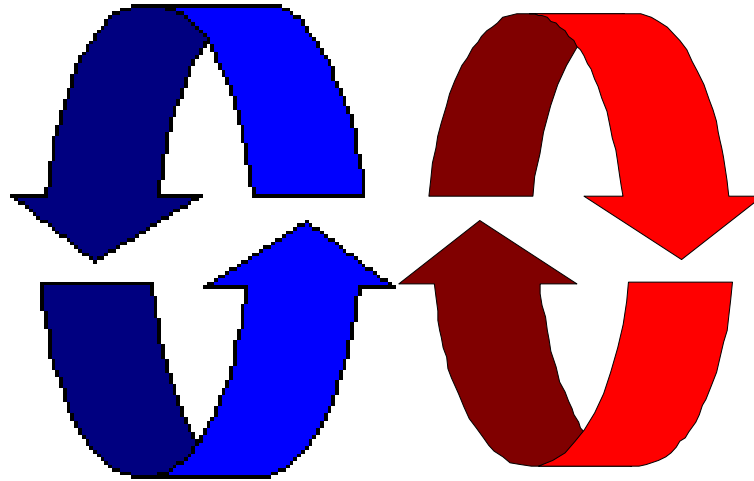# Concurrent Execution

Concurrent execution

Concepts: processes - concurrent execution
and interleaving.
process interaction.

Models: **parallel composition** of asynchronous processes
- interleaving
interaction - shared actions
process labeling, and action relabeling and hiding
structure diagrams

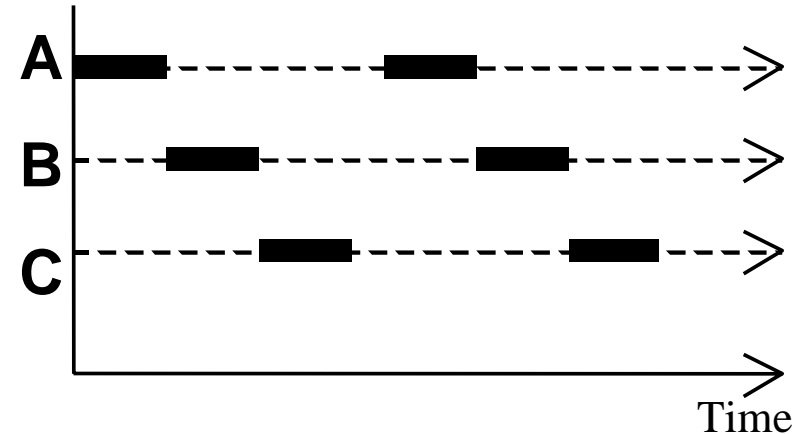**Practice**: Multithreaded Java programs

Definitions

◆ *Concurrency*

● *Logically* simultaneous processing. Does not imply multiple processing elements (PEs). Requires interleaved execution on a single PE.

◆ *Parallelism*

● *Physically* simultaneous processing. Involves multiple PEs and/or independent device operations.

Time

Both concurrency and parallelism require controlled access to shared resources . We use the terms parallel and concurrent interchangeably and generally do not distinguish between real and pseudo-concurrent execution.

3.1 Modeling Concurrency

◆ How should we model process execution speed?

- arbitrary speed

  (we abstract away time)

◆ How do we model concurrency?

- arbitrary relative order of actions from different processes

  (**interleaving** but preservation of each process order)

◆ What is the result?

- provides a general model independent of scheduling

  (**asynchronous** model of execution)

parallel composition - action interleaving

If P and Q are processes then (P||Q) represents the concurrent execution of P and Q. The operator || is the parallel composition operator.

```
ITCH  = (scratch->STOP).
CONVERSE = (think->talk->STOP).

||CONVERSE_ITCH = (ITCH || CONVERSE).
```
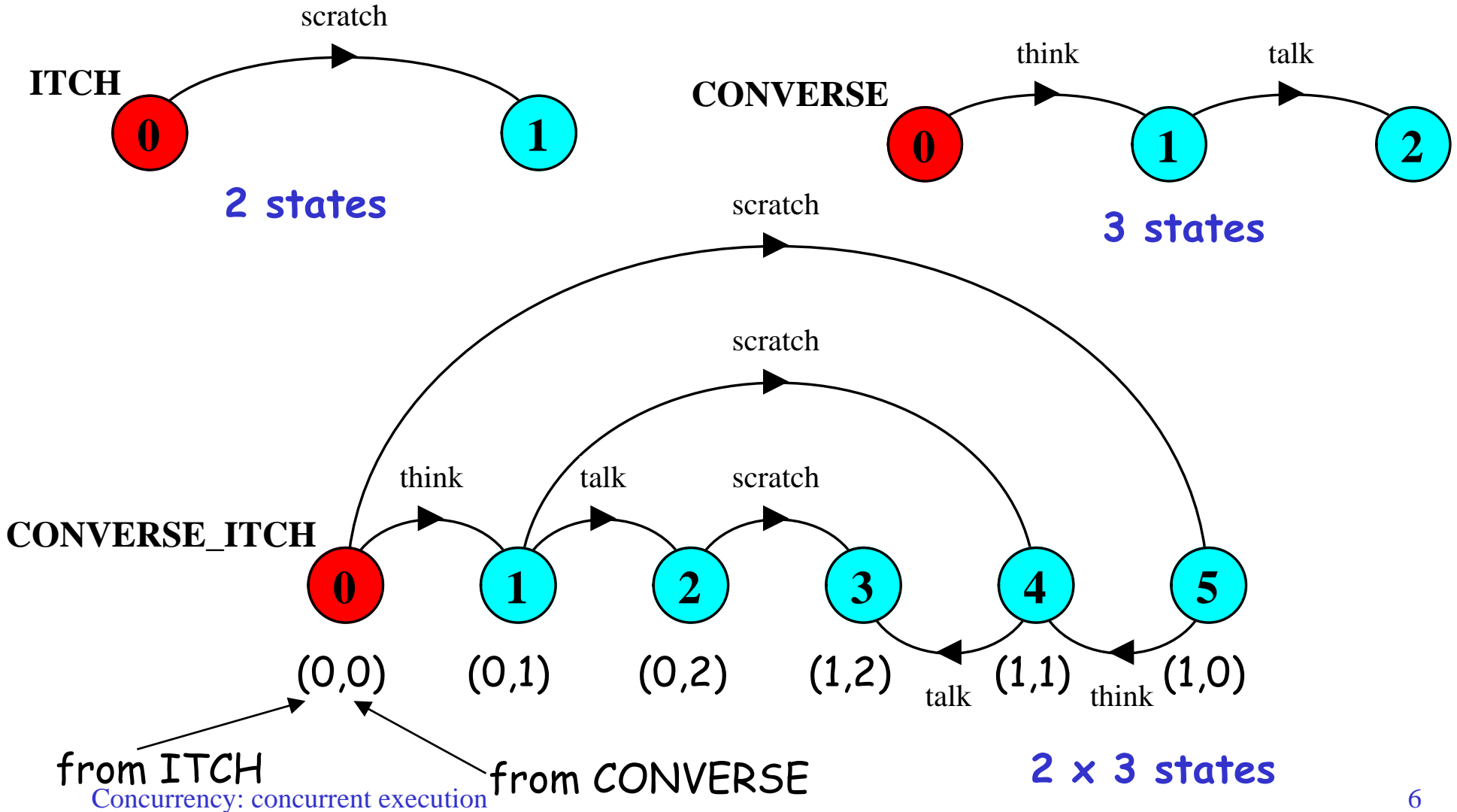
Disjoint alphabets

think→talk→scratch
think→scratch→talk
scratch→think→talk

Possible traces as a result of action interleaving.

parallel composition - action interleaving

ITCH

scratch

(0) → (1)

2 states

CONVERSE

think   talk

(0) → (1) → (2)

3 states

CONVERSE_ITCH

scratch

scratch

think   talk   scratch

(0) → (1) → (2) → (3)   (4)   (5)

talk   think

(0,0) (0,1) (0,2) (1,2) (1,1) (1,0)

from ITCH   from CONVERSE

2 x 3 states

parallel composition - algebraic laws

Commutative: `(P||Q) = (Q||P)`
Associative: `(P||(Q||R)) = ((P||Q)||R)`
                   `            = (P||Q||R).`

Clock radio example:

```
CLOCK = (tick->CLOCK).
RADIO = (on->off->RADIO).


||CLOCK_RADIO = (CLOCK || RADIO).
```

LTS?   Traces?   Number of states?

modeling interaction - shared actions

If processes in a composition have actions in common, these actions are said to be *shared*. Shared actions are the way that process interaction is modeled. While unshared actions may be arbitrarily interleaved, a shared action must be executed at the same time by all processes that participate in the shared action.

```
MAKER = (make->ready->MAKER).
USER  = (ready->use->USER).

||MAKER_USER = (MAKER || USER).
```

MAKER synchronizes with USER when ready.

LTS?   Traces?   Number of states?

Concurrency: concurrent execution

Non-disjoint alphabets

modeling interaction - handshake

A handshake is an action acknowledged by another:
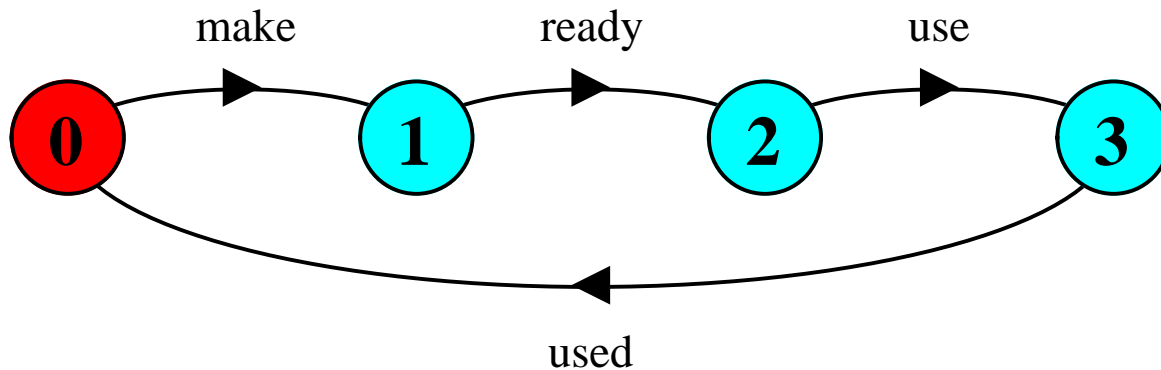
```
MAKERv2 = (make->ready->used->MAKERv2).
USERv2  = (ready->use->used ->USERv2).

||MAKER_USERv2 = (MAKERv2 || USERv2).
```

3 states
3 states

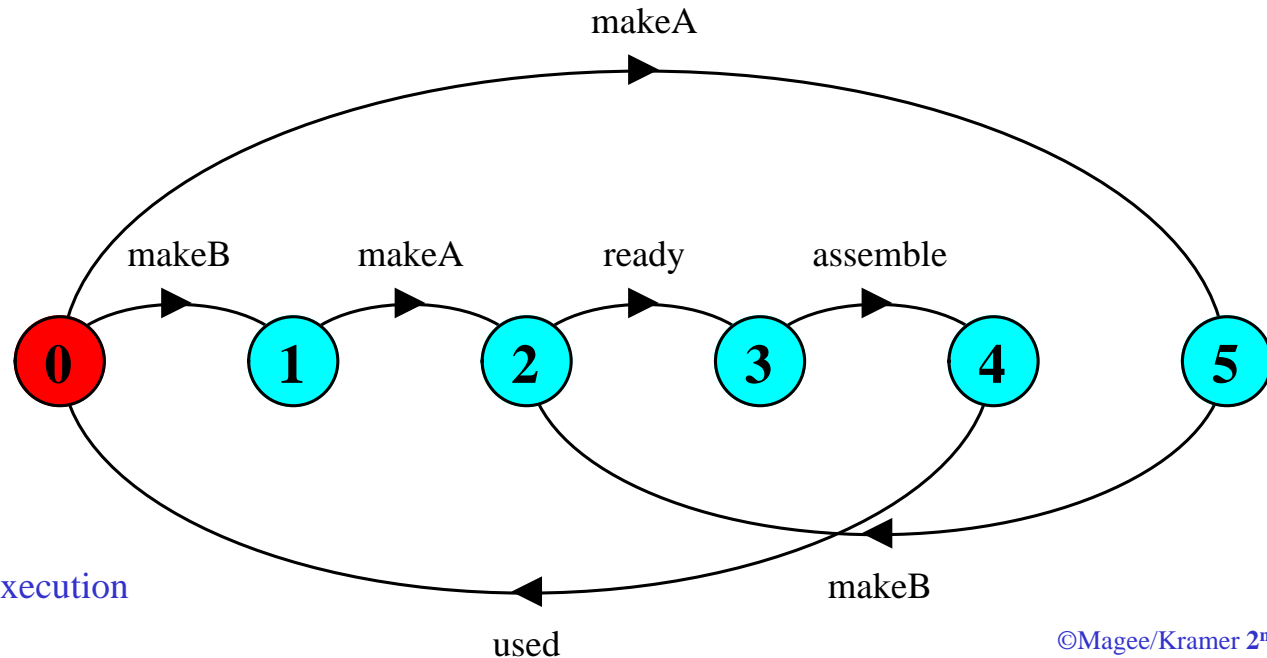3 x 3 states?

make   ready   use

used

4 states

Interaction **constrains** the overall behaviour.

modeling interaction - multiple processes

Multi-party synchronization:

```
MAKE_A    = (makeA->ready->used->MAKE_A).
MAKE_B    = (makeB->ready->used->MAKE_B).
ASSEMBLE = (ready->assemble->used->ASSEMBLE).

||FACTORY = (MAKE_A || MAKE_B || ASSEMBLE).
```

composite processes

A composite process is a parallel composition of primitive processes. These composite processes can be used in the definition of further compositions.

```
||MAKERS = (MAKE_A || MAKE_B).

||FACTORY = (MAKERS || ASSEMBLE).
```

Substituting the definition for **MAKERS** in **FACTORY** and applying the **commutative** and **associative** laws for parallel composition results in the original definition for **FACTORY** in terms of primitive processes.

```
||FACTORY = (MAKE_A || MAKE_B || ASSEMBLE).
```

process instances and labeling

a:P prefixes each action label in the alphabet of P with a.

Two **instances** of a switch process:

```
SWITCH =  (on->off->SWITCH).

||TWO_SWITCH = (a:SWITCH || b:SWITCH).
```

a:SWITCH

a.on

(0) → **(1)**

a.off

b:SWITCH

b.on

(0) → **(1)**

b.off
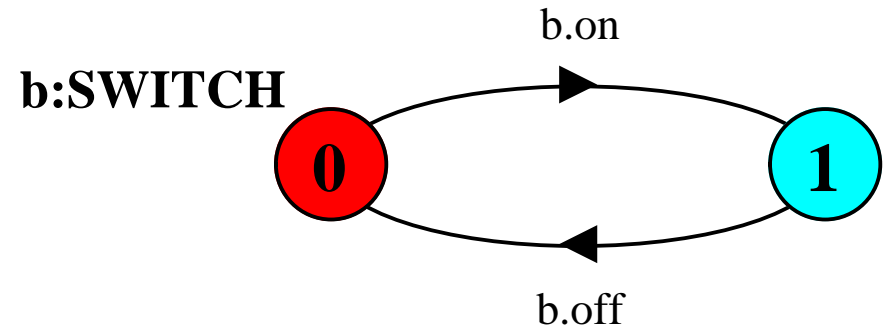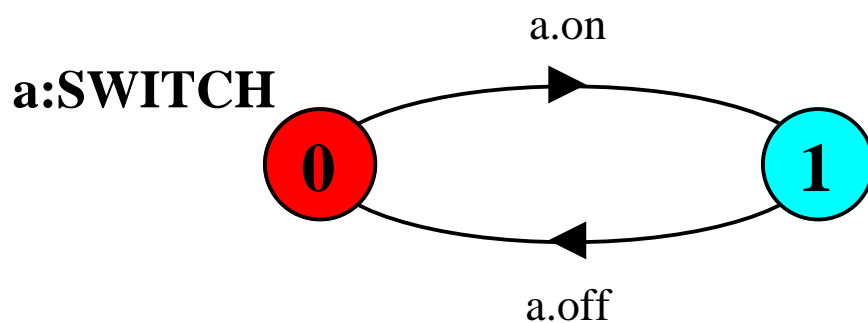
An array of **instances** of the switch process:

```
||SWITCHES(N=3) = (forall[i:1..N] s[i]:SWITCH).
||SWITCHES(N=3) = (s[i:1..N]:SWITCH).
```

process labeling by a set of prefix labels

{a1,..,ax}::P replaces every action label n in the alphabet of P with the labels a1.n,...,ax.n. Further, every transition (n->X) in the definition of P is replaced with the transitions ({a1.n,...,ax.n} ->X).

Process prefixing is useful for modeling **shared** resources:

```
RESOURCE = (acquire->release->RESOURCE).
USER = (acquire->use->release->USER).

||RESOURCE_SHARE = (a:USER  ||  b:USER
                       || {a,b}::RESOURCE).
```

process prefix labels for shared resources

a:USER

a.acquire   a.use

0 → 1 → 2

a.release

b:USER

b.acquire   b.use

0 → 1 → 2
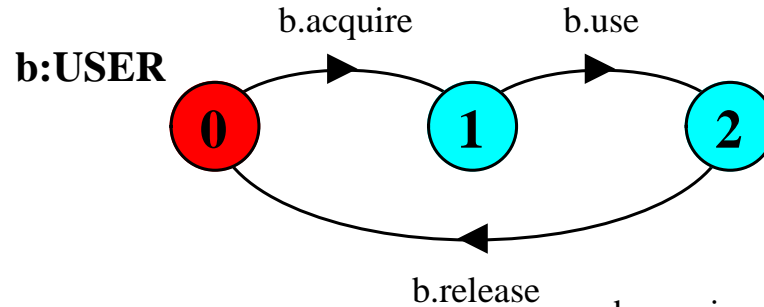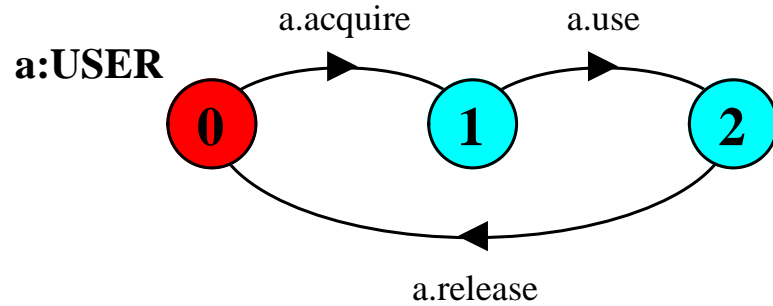
b.release

How does the model ensure that the user that acquires the resource is the one to release it?

{a,b}::RESOURCE

b.acquire
a.acquire

0 → 1

a.release
b.release

RESOURCE_SHARE

a.acquire

b.acquire   b.use   a.use

0   1   2   3   4

b.release

a.release
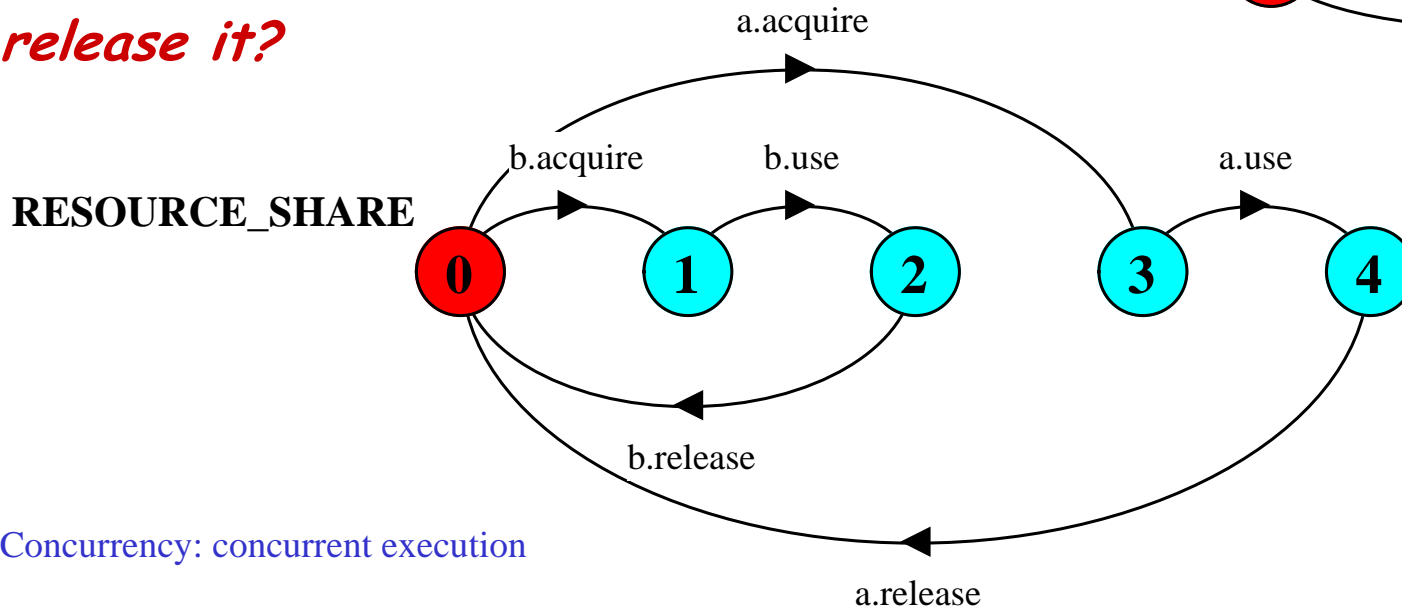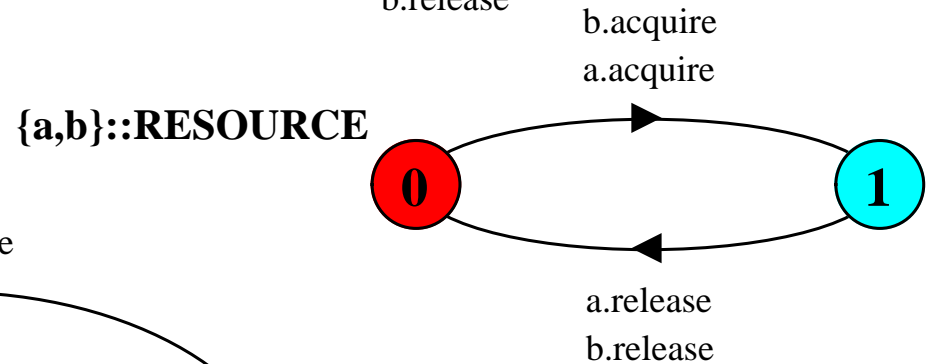
action relabeling

Relabeling functions are applied to processes to change the names of action labels. The general form of the relabeling function is:

/{*newlabel_1/oldlabel_1,... newlabel_n/oldlabel_n*}.

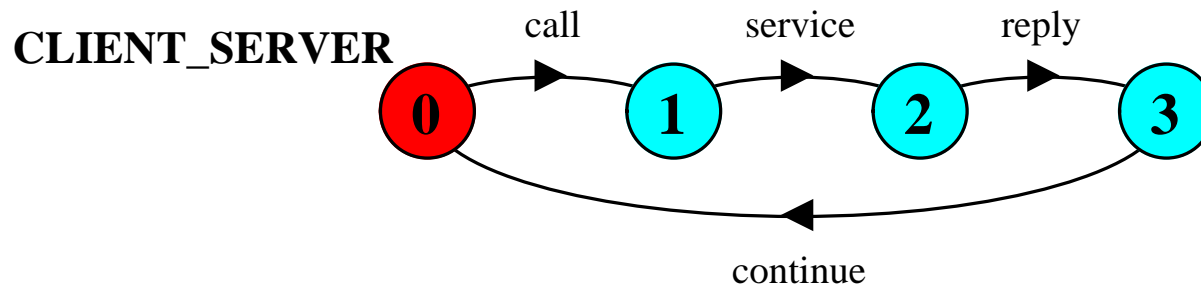Relabeling to ensure that composed processes synchronize on particular actions.

```
CLIENT = (call->wait->continue->CLIENT).
SERVER = (request->service->reply->SERVER).
```
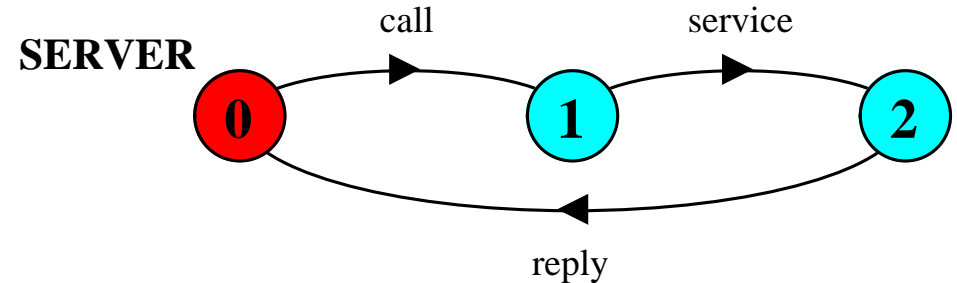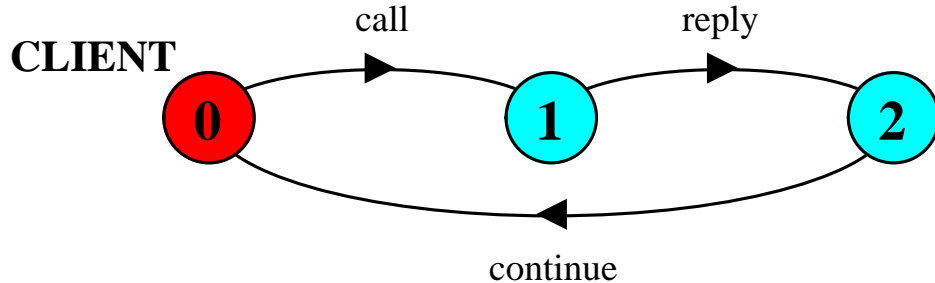
Note that both *newlabel* and *oldlabel* can be sets of labels.

action relabeling

```
||CLIENT_SERVER = (CLIENT || SERVER)
                   /{call/request, reply/wait}.
```

CLIENT

call — reply

0 → 1 → 2

continue

SERVER

call — service

0 → 1 → 2

reply

CLIENT_SERVER

call — service — reply

0 → 1 → 2 → 3

continue

action relabeling - prefix labels

An alternative formulation of the client server system is described below using qualified or prefixed labels:

```
SERVERv2 = (accept.request
             ->service->accept.reply->SERVERv2).
CLIENTv2 = (call.request
             ->call.reply->continue->CLIENTv2).


||CLIENT_SERVERv2 = (CLIENTv2 || SERVERv2)
                    /{call/accept}.
```

action hiding - abstraction to reduce complexity

When applied to a process P, the hiding operator \{a1..ax} removes the action names a1..ax from the alphabet of P and makes these concealed actions "silent". These silent actions are labeled tau. Silent actions in different processes are not shared.

Sometimes it is more convenient to specify the set of labels to be exposed....

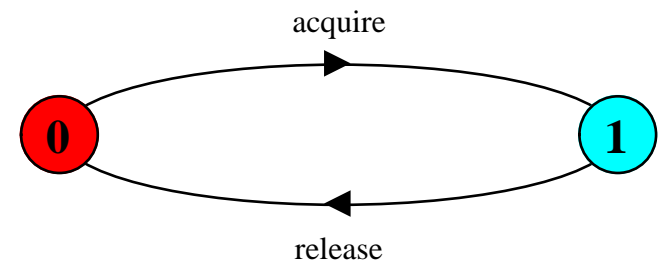When applied to a process P, the interface operator @{a1..ax} hides all actions in the alphabet of P not labeled in the set a1..ax.
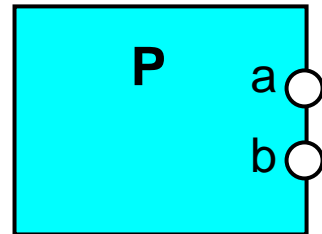
action hiding

The following definitions are equivalent:

```
USER = (acquire->use->release->USER)
        \{use}.
```

```
USER = (acquire->use->release->USER)
          @{acquire,release}.
```
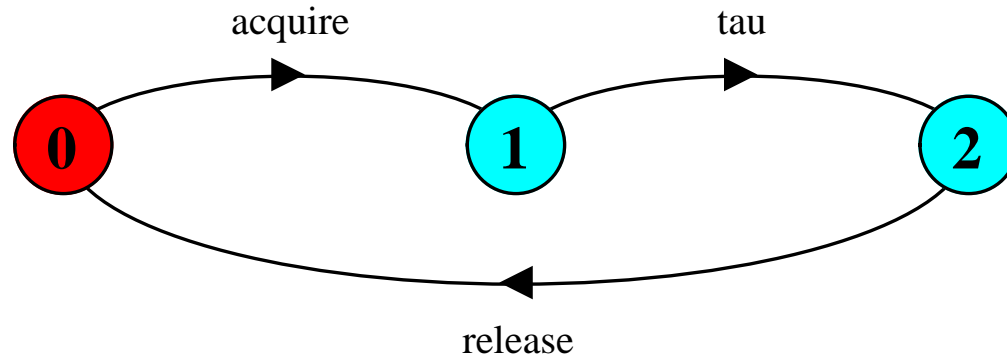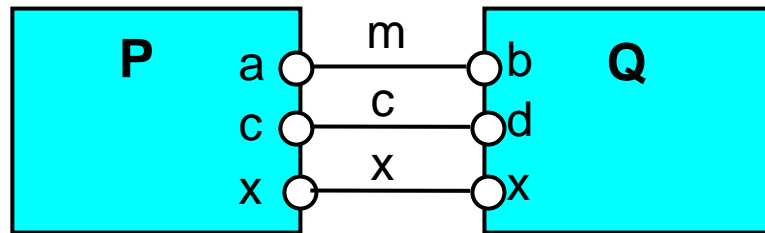

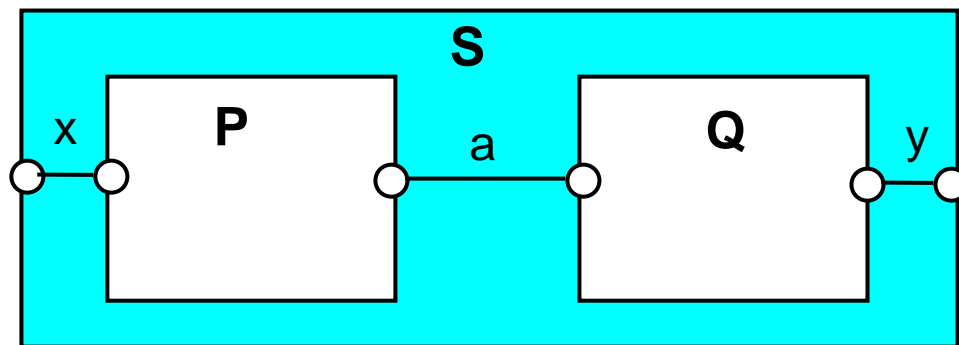Minimization removes hidden **tau** actions to produce an LTS with equivalent observable behavior.

structure diagrams – systems as interacting processes

Process P with
alphabet {a,b}.

Parallel Composition
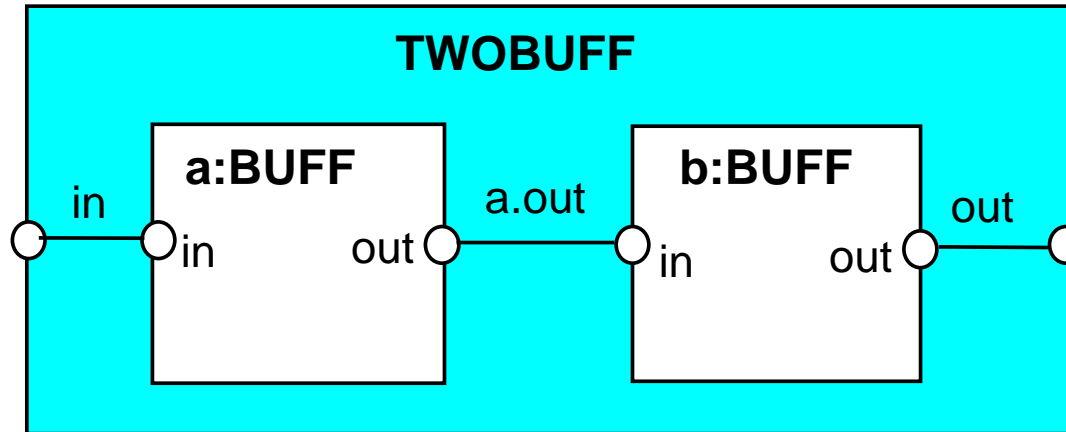(P||Q) / {m/a,m/b,c/d}

Composite process
||S = (P||Q) @ {x,y}

structure diagrams

We use structure diagrams to capture the structure of a model expressed by the static combinators: *parallel composition, relabeling* and *hiding.*
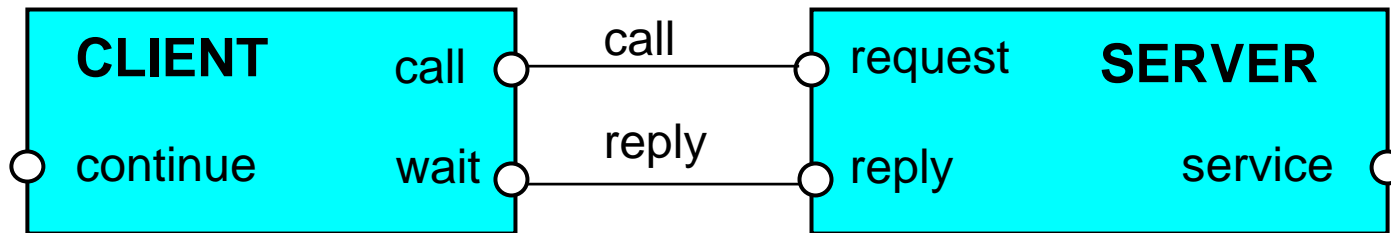
```
range T = 0..3
BUFF = (in[i:T]->out[i]->BUFF).

||TWOBUF = ?
```
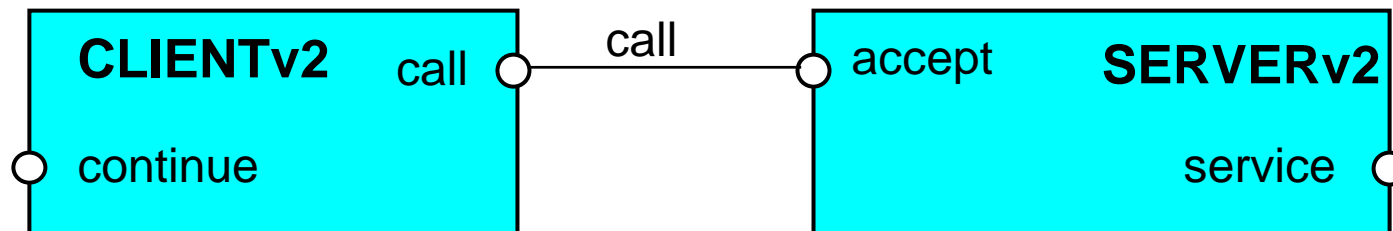
structure diagrams

Structure diagram for `CLIENT_SERVER` ?

Structure diagram for `CLIENT_SERVERv2` ?

structure diagrams - resource sharing

PRINTER_SHARE

a:USER
printer ○

printer: RESOURCE
○ acquire
○ release
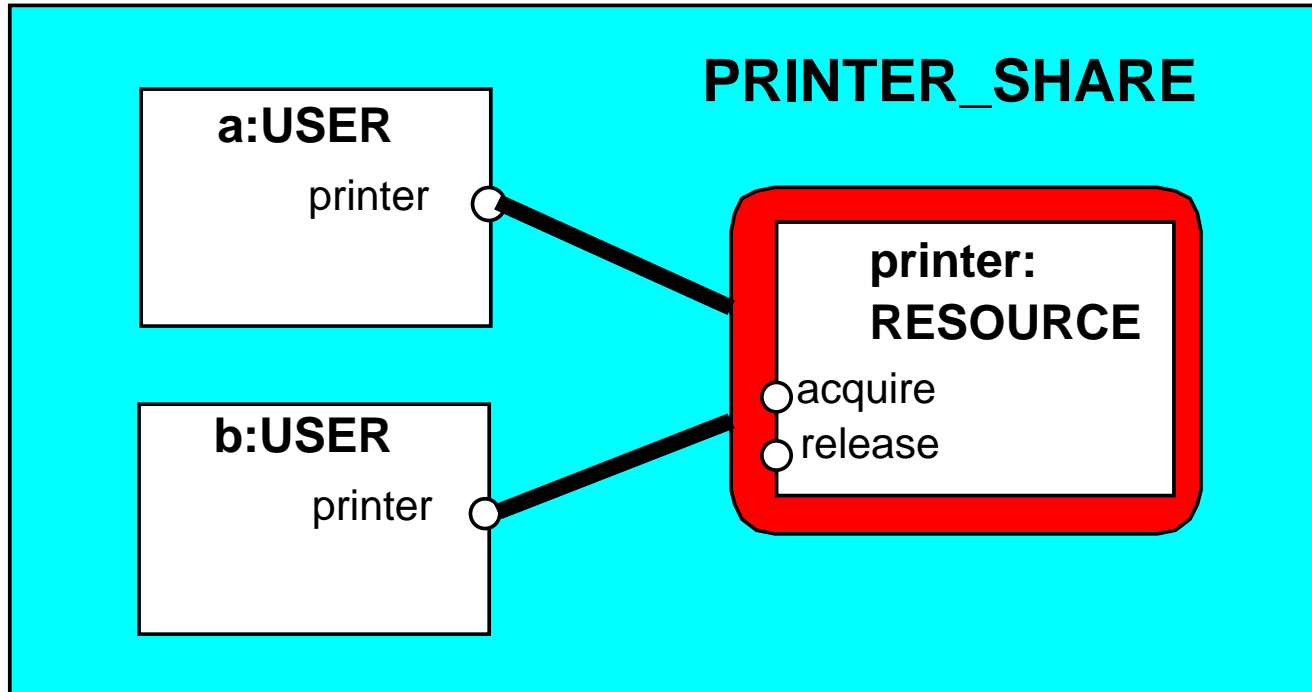
b:USER
printer ○

```
RESOURCE = (acquire->release->RESOURCE).
USER =      (printer.acquire->use
            ->printer.release->USER)\{use}.

||PRINTER_SHARE
  = (a:USER||b:USER||{a,b}::printer:RESOURCE).
```
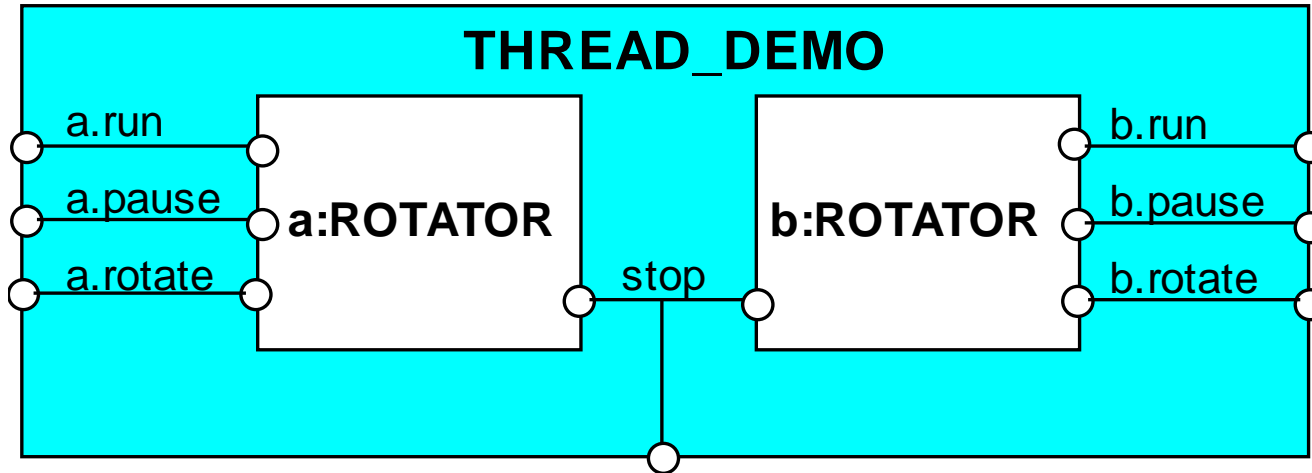
3.2 Multi-threaded Programs in Java

Concurrency in Java occurs when more than one thread is alive. ThreadDemo has two threads which rotate displays.

ThreadDemo model

THREAD_DEMO

a.run

a.pause   **a:ROTATOR**

a.rotate

stop   **b:ROTATOR**

b.run
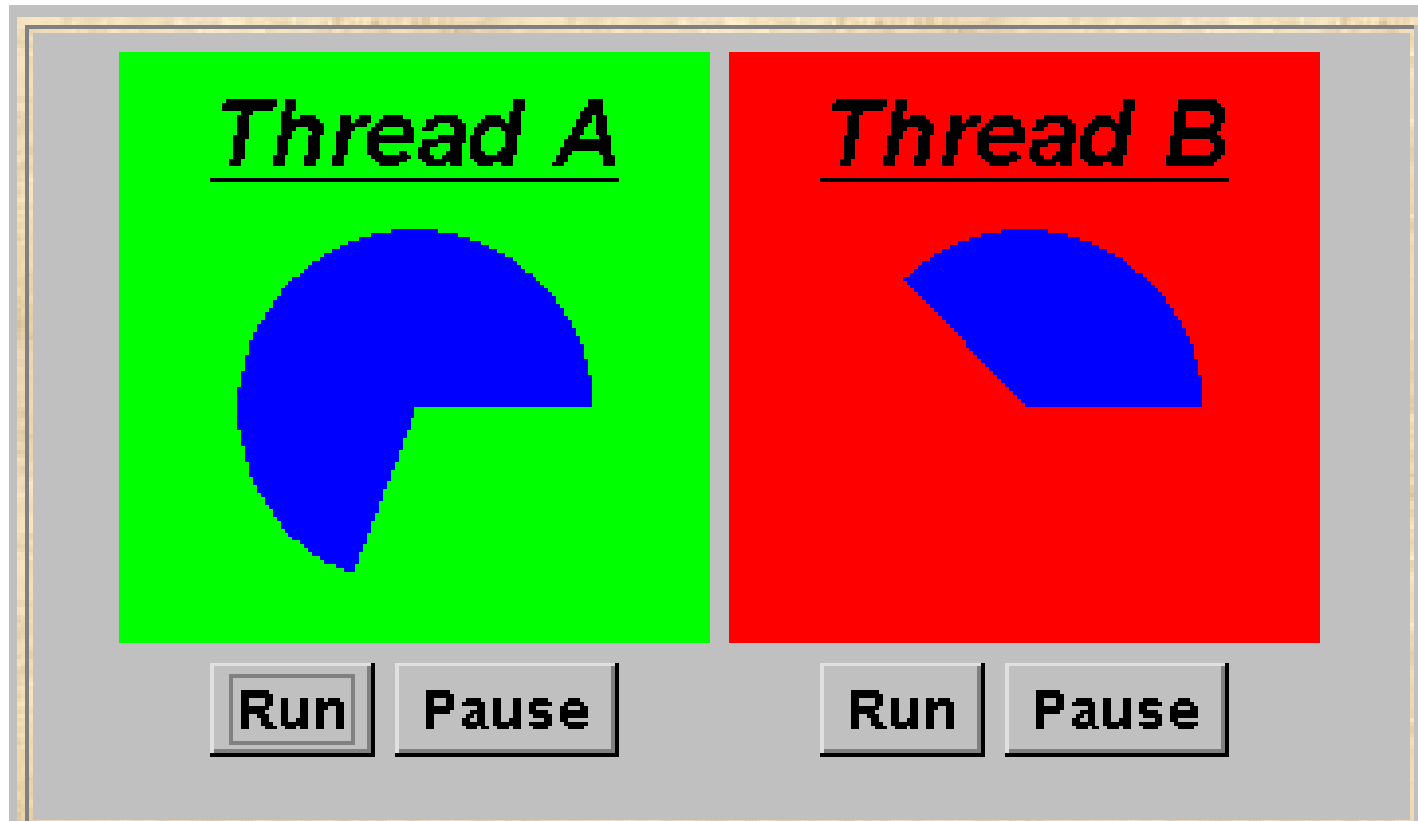
b.pause

b.rotate

```
ROTATOR = PAUSED,
PAUSED  = (run->RUN | pause->PAUSED
          |interrupt->STOP),
RUN     = (pause->PAUSED |{run,rotate}->RUN
          |interrupt->STOP).

||THREAD_DEMO = (a:ROTATOR || b:ROTATOR)
 /{stop/{a,b}.interrupt}.
```
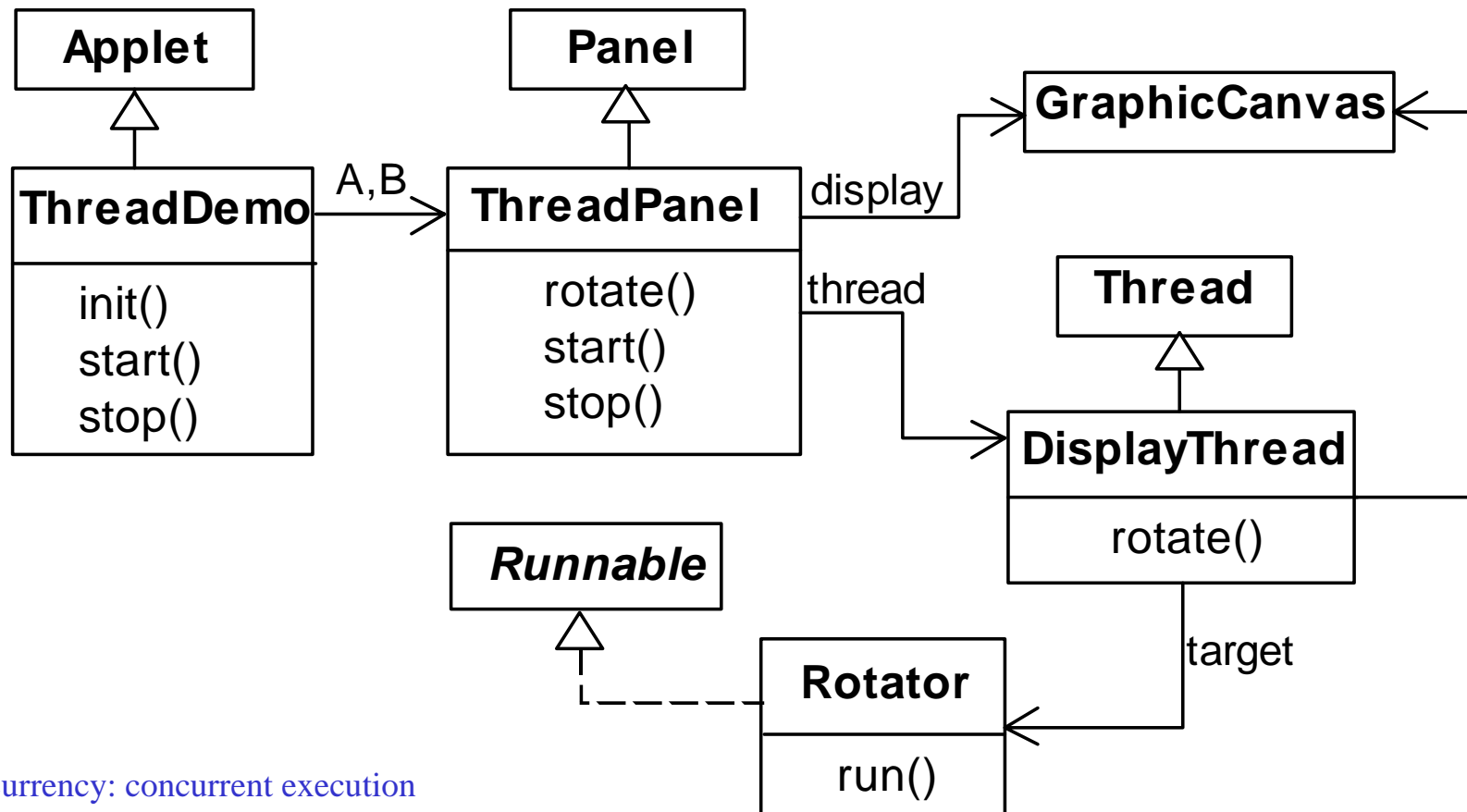
Interpret `run,` `pause,` `interrupt` *as inputs,* `rotate` *as an output.*

ThreadDemo implementation in Java - class diagram

ThreadDemo creates two **ThreadPanel** displays when initialized.
ThreadPanel manages the display and control buttons, and delegates calls to
rotate() to **DisplayThread**. **Rotator** implements the **runnable** interface.

Rotator class

```
class Rotator implements Runnable {

  public void run() {
    try {
      while(true) ThreadPanel.rotate();
    } catch(InterruptedException e) {}
  }
}
```

Rotator implements the **runnable** interface, calling **ThreadPanel.rotate()** to move the display.

run() finishes if an exception is raised by **Thread.interrupt()**.

ThreadPanel class

```java
public class ThreadPanel extends Panel {

  // construct display with title and segment  color c
  public ThreadPanel(String title, Color c) {…}

  // rotate display of currently running thread 6 degrees
  // return value not used in this example
  public static boolean rotate()
        throws InterruptedException {…}

  // create a new thread with target r and start it running
  public void start(Runnable r) {
       thread = new DisplayThread(canvas,r,…);
       thread.start();
   }

  // stop the thread using Thread.interrupt()
  public void stop() {thread.interrupt();}
}
```

Calls to **rotate()** are delegated to **DisplayThread**.

Threads are created by the **start()** method, and terminated by the **stop()** method.

ThreadDemo class

```java
public class ThreadDemo extends Applet {
  ThreadPanel A; ThreadPanel B;

  public void init() {
    A = new ThreadPanel("Thread A",Color.blue);
    B = new ThreadPanel("Thread B",Color.blue);
    add(A); add(B);
  }

  public void start() {
    A.start(new Rotator());
    B.start(new Rotator());
  }

  public void stop() {
    A.stop();
    B.stop();
  }
}
```

ThreadDemo creates two **ThreadPanel** displays when initialized and two threads when started.

ThreadPanel is used extensively in later demonstration programs.

Summary

◆ Concepts

- **concurrent processes and process interaction**

◆ Models

- **Asynchronous** (arbitrary speed) **& interleaving** (arbitrary order).
- **Parallel composition** as a finite state process with action interleaving.
- **Process interaction** by shared actions.
- Process labeling and action relabeling and hiding.
- **Structure diagrams**

◆ Practice

- **Multiple threads** in Java.