

# Array Distribution Schemes

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# Outline

Block distributions

2D distribution

Cyclic and block-cyclic distributions

# Block distributions

- ▶ Each process receives a contiguous part of the data
- ▶ Suitable when there is a locality in the interactions
- ▶ E.g. distributing an  $n \times n$  matrix
  - ▶ row-wise distribution: each process receives  $\approx n/p$  rows of the matrix
  - ▶ column-wise distribution: each process receives  $\approx n/p$  columns of the matrix
  - ▶ suitable e.g. for matrix-vector multiplication

## 2D distribution

- ▶ Assume a process grid of size  $p_1 \times p_2$   
Number of processes is  $p = p_1 p_2$
- ▶ Consider distributing an  $n \times n$  matrix
  - ▶ We can split it into  $n/p_1 \times n/p_2$  sub matrices

4 × 4 process grid

$P_0$	$P_1$	$P_2$	$P_3$
$P_4$	$P_5$	$P_6$	$P_7$
$P_8$	$P_9$	$P_{10}$	$P_{11}$
$P_{12}$	$P_{13}$	$P_{14}$	$P_{15}$

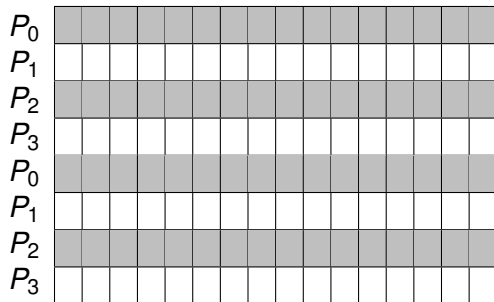
2 × 4 process grid

$P_0$	$P_1$	$P_2$	$P_3$
$P_4$	$P_5$	$P_6$	$P_7$

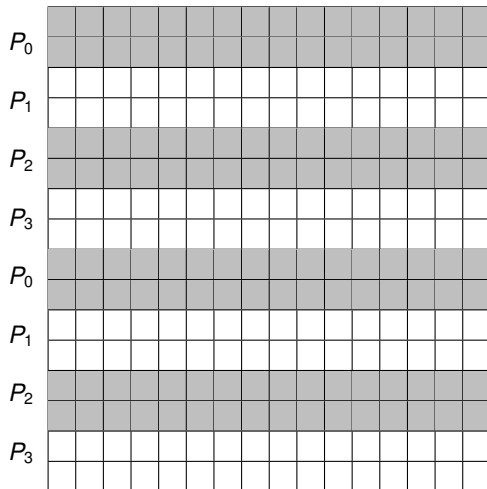
## Cyclic and block-cyclic distributions

- ▶ If the amount of work is different for different parts of a matrix, this could lead to load imbalances
- ▶ One way to avoid this is to use cyclic or block-cyclic distributions

## 1D cyclic distribution on 4 processes



# 1D block-cyclic distribution of 4 processes



## 2D distribution on 4 processes

$P_0$	$P_1$	$P_0$	$P_1$
$P_2$	$P_3$	$P_2$	$P_3$
$P_0$	$P_1$	$P_0$	$P_1$
$P_2$	$P_3$	$P_2$	$P_3$