## Shared Objects and Mutual Exclusion CS 2SD3

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Shared Objects & Mutual Exclusion

Concepts: process interference. mutual exclusion and locks.

Models: model checking for interference modelling mutual exclusion

Practice: thread interference in shared Java objects mutual exclusion in Java (synchronized objects/methods).

## Ornamental garden problem:

• People enter an ornamental garden through either of two turnstiles. Management wish to know how many are in the garden at any time.



• Suppose that movement of people is modeled by two concurrent processes and a '*shared*' counter.

## First Solution to The Garden Problem

- Simplification: Nobody leaves the garden
- Technique: Busy Waiting
- We have to implement counting!
- Structure Diagram of Ornamental Garden:



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```
const N = 4
                                                 The alphabet of shared
range T = 0...N
                                                 process VAR is declared
set VarAlpha = { value.{read[T],write[T]} }
                                                 explicitly as a set
VAR = VAR[0],
                                                 constant, VarAlpha.
VAR[u:T] = (read[u] ->VAR[u])
            write[v:T]->VAR[v]).
                                                   The TURNSTILE
TURNSTILE = (go -> RUN),
                                                   alphabet is extended
          = (arrive-> INCREMENT
RUN
                                                   with VarAlpha to
             lend -> TURNSTILE) ,
                                                   ensure no unintended
INCREMENT = (value.read[x:T])
                                                   free (autonomous)
              -> value.write[x+1]->RUN
                                                   actions in VAR such as
             )+VarAlpha.
                                                   value.write[0].
||GARDEN = (east:TURNSTILE || west:TURNSTILE
            || { east,west,display}::value:VAR)
                                                   All actions in the
             /{ go /{ east,west} .go,
                                                   shared VAR must be
               end/{ east,west} .end} .
                                                   controlled (shared) by
```

- a **TURNSTILE**.
- *go*/{*east*, *west*}.*go* means *east*.*go* and *west*.*go* are <u>the same</u> as action *go*.
- *go*/{*east*, *west*}.*end* means *east*.*end* and *west*.*end* are <u>the same</u> action as *end*.
- but east.arrive and west.arrive are distinct!

•  $\{east, west, display\}$  :: value : VAR implies: value : VAR = value : VAR[0] value :  $VAR[u : T] = (value.read[u] \rightarrow value$  : VAR[u] |  $value.write[v : T] \rightarrow value$  : VAR[c]) =( $east.value.read[u] \rightarrow value$  : VAR[u] |  $west.value.read[u] \rightarrow value$  : VAR[u] |  $display.value.read[u] \rightarrow value$  : VAR[u] |  $east.value.write[v : T] \rightarrow value$  : VAR[v] |  $west.value.write[v : T] \rightarrow value$  : VAR[v] | $display.value.write[v : T] \rightarrow value$  : VAR[v] |

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• Consider a trace:

 $go \rightarrow east.arrive \rightarrow east.value.read[0] \rightarrow west.arrive \rightarrow west.value.read[0] \rightarrow east.value.write[1] \rightarrow west.value.write[1] \rightarrow end \rightarrow display.value.read[1]$ 

- We have **two** people in the garden but the counter displays number 1!
- *west.value.read*[0] was executed *before east.value.write*[1], so *VAR* did not update storage!
- The trace below is OK.

 $go \rightarrow east.arrive \rightarrow east.value.read[0] \rightarrow east.value.write[1] \rightarrow west.arrive \rightarrow west.value.read[1] \rightarrow west.value.write[2] \rightarrow end \rightarrow display.value.read[2]$ 

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- How can we find such errors?
- Exhoustive checking, a kind of model checking, software support needed
- **TEST:** a process which summs the arrivals and checks against the display value

```
TEST
            = \text{TEST}[0],
TEST[v:T]
             =
      (when (v<N) {east.arrive, west.arrive} ->TEST[v+1]
      |end->CHECK[v]
CHECK[v:T] =
                                                Like STOP, ERROR
     (display.value.read[u:T] ->
                                                is a predefined FSP
        (when (u==v) right -> TEST[v]
                                                local process (state),
        |when (u!=v) wrong -> ERROR
                                                numbered - I in the
                                                equivalent LTS.
    )+{display.VarAlpha}.
```

 $TESTGARDEN = (GARDEN \parallel TEST)$ 

• LTSA will produce the red trace form page 7 followed by 'wrong'

- Destructive update, caused by the arbitrary interleaving of read and write type actions, is termed INTERFERENCE.
- Interference bugs are extremely difficult to locate.
- The general solution is to use **MUTUAL EXCLUSION**.

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# Modeling Mutual Exclusion

• To add locking to our model, define a LOCK, compose it with the shared VAR in the garden, and modify the alphabet set :

• Modify TURNSTILE to acquire and release the lock:

TURNSTILE	=	$(go \rightarrow RUN)$ ,
RUN	=	(arrive-> INCREMENT
		end -> TURNSTILE) ,
INCREMENT	=	(value.acquire
		-> value.read[x:T]->value.write[x+1]
		-> value. <mark>release</mark> ->RUN
		)+VarAlpha.

• Old INCREMENT:  $INCREMENT = (value.read[x : T] \rightarrow value.write[x + 1] \rightarrow RUN)$ + VarAlpha

#### • Trace:

 $go \rightarrow east.arrive \rightarrow east.value.acquire \rightarrow east.value.read[0] \rightarrow east.value.write[1] \rightarrow east.value.release \rightarrow west.arrive \rightarrow west.value.acquire \rightarrow west.value.read[1] \rightarrow west.value.write[2] \rightarrow west.value.release \rightarrow end \rightarrow display.value.read[2].$ 

- We can test it similarly as previously using TEST process and LTSA.
- But tests cannot prove correctness, only can find errors!

### Abstraction using action hiding



- Is the model discussed really necessary?
- Can it be specified in a much more simpler way?
- What about this:

 $TURNSTILES\_GUARD = (check \rightarrow (east.arrive \rightarrow push\_button \rightarrow TURNSTILE\_GUARD | west.arrive \rightarrow push\_button \rightarrow TURNSTILE\_GUARD | none \rightarrow TURNSTILE\_GUARD)$ 

 $\begin{array}{l} \textit{COUNTER\_TO\_4} = \textit{push\_button} \rightarrow +1 \rightarrow \textit{push\_button} \rightarrow +1 \rightarrow \textit{push\_button} \rightarrow +1 \rightarrow \textit{push\_button} \rightarrow +1 \rightarrow \textit{STOP} \end{array}$ 

 $\parallel GARDEN = (TURNSTILES_GUARD \parallel COUNTER_TO_4)$ 

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## Petri Nets Versions

TURNSTILES\_GUARD (two versions):



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## Composed Net



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- Suppose that the garden we have considered is a sacred garden of some cult that worship '*simultaneity*'. Hence it has two counters, one that counts all worshipers in the garden, and the other that only counts those blessed events when two people enter simultaneously from both the east and the west entrances.
- Assume that this event is somehow observable, for instance openings og gates are synchronized, etc.
- Can you model this new garden in terms of FSP? If 'yes', how, as we have interleavings only in this model?